## PROPOSED DRAFT FOR PUBLIC COMMENT

2020 WYOMING MATH EXTENDED STANDARDS and ACHIEVEMENT LEVEL DESCRIPTORS (ALDs)

Standards and ALDs for students with significant cognitive disabilities.


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Effective - XXX, 2020

TO BE FULLY IMPLEMENTED IN DISTRICTS BY THE BEGINNING OF SCHOOL YEAR 2023-24

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (AL |
| :---: | :---: | :---: |
| Counting and Cardinality | Grade K |  |
| Know number names and the count sequence. (A) <br> K.CC.A. 1 Count to 100 by ones and by tens. <br> A. Count to 100 by ones and by tens. <br> B. Count backwards by ones from 20. | EEK.CC.A. 1 Starting with one, count to 10 by ones. | Level IV AA Students will: <br> EEK.CC.A. 1 Starting with one, count to 20 by ones. <br> Level III AA Students will: <br> EEK.CC.A. 1 Starting with one, count to 10 by ones. <br> Level II AA Students will: <br> EEK.CC.A. 1 Starting with one, count by ones to five. <br> Level I AA Students will: <br> EEK.CC.A. 1 Count from one to two. |
| K.CC.A. 2 Count forward beginning from a given number within the known sequence (instead of having to begin at 1). | EEK.CC.A. 2 Count forward from a given number in a known sequence between 2 and 20. | Level IV AA Students will: <br> EEK.CC.A. 2 Count forward from 19 to 30. <br> Level III AA Students will: <br> EEK.CC.A. 2 Count forward from a given number in a known sequence between 2 and 20. <br> Level II AA Students will: <br> EEK.CC A. 2 Count forward from a given number in a known sequence between 2 and 10. <br> Level I AA Students will: <br> EEK.CC.A. 2 Count forward from 2 to 4. |
| K.CC.A. 3 Write numbers from 0 to 20. Represent a number of objects with a written numeral 0-20 (with 0 (Zero) representing a count of no objects). | EEK.CC.A. 3 Count a number of objects and match with the numerical symbol 1-10. | Level IV AA Students will: <br> EEK.CC.A. 3 Count a given number of objects between 1-10 and write the numerical symbol. <br> Level III AA Students will: <br> EEK.CC.A. 3 Count a number of objects and match with the numerical symbol 1-10. <br> Level II AA Students will: <br> EEK.CC.A. 3 Match the numerical symbol to a quantity of objects up to 5 . <br> Level I AA Students will: <br> EEK.CC.A. 3 Match the numerical symbol to a quantity of objects up to 2. |
| Count to tell the number of objects. (B) <br> K.CC.B. 4 Understand the relationship between numbers and quantities; connect counting to cardinality. <br> A. Use one-to-one correspondence whe counting objects. | EEK.CC.B. 4 <br> Demonstrate one-toone correspondence, by counting 10 objects. | Level IV AA Students will: <br> EEK.CC.B. 4 Demonstrate one-to-one correspondence counting any number of objects within 10 and show one more or one less. <br> Level III AA Students will: <br> EEK.CC.B. 4 Demonstrate one-to-one correspondence, by counting 10 objects. <br> Level II AA Students will: <br> EEK.CC.B. 4 Demonstrate one-to-one correspondence by counting 5 objects. Level I AA Students will: |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

B. Understand that the last number name said, tells the number of objects counted regardless of their arrangement.
C. Understand that each successive number name refers to a quantity that is one more, and each previous number name refers to a quantity that is one less.
K.CC.B. 5 When counting:
A. Answer the question "how many?" by counting up to 20 objects arranged in a line, a rectangular array, a circle, or as many as 10 objects in a scattered configuration
B. Given a number from 1-20 count out that many objects.

## Compare numbers. (C)

K.CC.C. 6 Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group. (Include groups with up to ten objects.)

## EEK.CC.B. 5 Answer

 the question "how many?" by counting 10 objects arranged in a line or 5 objects in a scattered configuration.
## EEK.CC.C. 6 Given two

 groups of different quantities of objects, identify which group has more or less. (Include groups with up to 7 objects.)EEK.CC.B. 4 Demonstrate one-to-one correspondence by counting 2 objects.

## Level IV AA Students will:

EEK.CC.B. 5 Given a number between 1-10, count out that many objects.
Level III AA Students will:
EEK.CC.B. 5 Answer the question "how many?" by counting 10 objects arranged in a line or 5 objects in a scattered configuration.
Level II AA Students will:
EEK.CC.B. 5 Answer the question "how many?" by counting 5 objects arranged in a line or 3 objects in a scattered configuration.

## Level I AA Students will:

EEK.CC.B. 5 Answer the question "how many?" by counting 2 objects.
Level IV AA Students will:
EEK.CC.C. 6 Given two groups of different quantities of objects, identify which group has more, less, or equal. (Include groups with up to 7 objects.)

## Level III AA Students will:

EEK.CC.C. 6 Given two groups of different quantities of objects, identify which group has more or less. (Include groups with up to 7 objects.)
Level II AA Students will:
EEK.CC.C. 6 Given two groups of different quantities of objects, identify which group has more. (With groups up to 7 objects).
Level I AA Students will:
EEK.CC.C. 6 Given a group of one and a group of 7 objects, identify which group has more.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

K.CC.C. 7 Compare two numbers between 1 and 10 presented as written numerals.

## 2018 Wyoming Mathematics

 Content StandardsOperations and Algebraic Thinking
Understand addition as putting together and adding to, and understand subtraction as taking apart and taking from. (D)
K.OA.D. 1 Model situations that involve representing addition and subtraction with objects, fingers, mental images, drawings, sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations.
K.OA.D. 2 Solve word problems using objects and drawings to find sums up to 10 and differences within 10.

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EEK.CC.C. 7 Compare
two numerical symbols
between 1-6 to
determine more or less.

## 2020 Wyoming Math

 Extended Standards
## Grade K

EEK.OA.D. 1
Demonstrate addition as "putting together" or subtraction as "taking from" with quantities to 5.

EEK.OA.D. 2 Using word problems, demonstrate addition as "putting together" or subtraction as "taking from" with quantities to 5.

Level IV AA Students will:
EEK.CC.C. 7 Compare two numerical symbols between 1-8 to determine more and less.
Level III AA Students will:
EEK.CC.C. 7 Compare two numerical symbols between 1-6 to determine more or less.
Level II AA Students will:
EEK.CC.C. 7 Compare two numerical symbols between 1-4 to determine which has more.
Level I AA Students will:
EEK.CC.C. 7 Given the numerical symbols " 1 " and " 2 " determine which is more
Instructional Achievement Level Descriptor (ALDs)

## Level IV AA Students will:

EEK.OA.D. 1 Demonstrate addition as "putting together" and subtraction as "taking from" with quantities to 10.
Level III AA Students will:
EEK.OA.D. 1 Demonstrate addition as "putting together" or subtraction as "taking from" with quantities to 5.
Level II AA Students will:
EEK.OA.D. 1 Follow directions to "put together" by adding 1 and "take from" by taking away 1.
Level I AA Students will:
EEK.OA.D. 1 Follow directions to "put together" by adding 1.

## Level IV AA Students will:

EEK.OA.D. 2 Using word problems, demonstrate addition as "putting together" or subtraction as "taking from" with quantities to 7
Level III AA Students will:
EEK.OA.D. 2 Using word problems, demonstrate addition as "putting together" or subtraction as "taking from" with quantities to 5.

## Level II AA Students will:

EEK.OA.D. 2 Using word problems, demonstrate addition as "putting together" by adding one and subtraction as "taking from" by taking away 1.

## Level I AA Students will:

EEK.OA.D. 2 Using word problems, demonstrate addition as "putting together" by adding one.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

K.OA.D. 3 Decompose numbers less than or equal to 10 in more than one way.
K.OA.D. 4 For any number from 1 to 9, find the number that makes 10 when added to the given number.
K.OA.D. 5 Fluently add and subtract within 5 .

## 2018 Wyoming Mathematics

Content Standards
Number and Operation Base Ten
Work with numbers 11-19 to gain foundations for place value. (E)
K.NBT.E. 1 Describe, explore, and explain how the counting numbers 11 to 19 is:
A. Composed of ten ones and more ones.
B. Decomposed into ten ones and more ones.

EEK.OA.D. 3
Decompose numbers into sub-parts to equal 5.

EEK.OA.D. 4 For any number from 1 to 4, find the number that makes 5 when added to the given number.

EEK.OA.D. 5 Not applicable.

## 2020 Wyoming Math

 Extended Standards
## Grade K

EEK.NBT.E. 1 Explore how the counting numbers between 6-10 is composed of 5 ones and more ones.

Level IV AA Students will:
EEK.OA.D. 3 Decompose numbers less than or equal to 5 in more than one way.
Level III AA Students will:
EEK.OA.D. 3 Decompose numbers into sub-parts to equal 5.
Level II AA Students will:
EEK.OA.D. 3 Decompose numbers into sub-parts to equal 3.
Level I AA Students will:
EEK.OA.D. 3 Match sub-parts for a sum less than 3.
Level IV AA Students will:
EEK.OA.D. 4 For any number from 1 to 6 , find the number that makes 7 when added to the given number.
Level III AA Students will:
EEK.OA.D. 4 For any number from 1 to 4 , find the number that makes 5 when added to the given number.
Level II AA Students will:
EEK.OA.D. 4 For the numbers 1 or 2, find the number that makes 3 when added to the given number.
Level I AA Students will:
EEK.OA.D. 4 Natch the numbers 1 and 2, to show the sum 3.
***The Extended Standards Educator Committee determined there are no realworld applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EEK.NBT.E. 1 Explore how counting numbers 6-10 is decomposed into 5 ones and more ones.
Level III AA Students will:
EEK.NBT.E. 1 Explore how counting numbers between 6-10 is composed of 5 ones and more ones.
Level II AA Students will:
EEK.NBT.E. 1 Demonstrate how the numbers 6 and 7 are composed of 5 ones and more ones.

## Level I AA Students will:

EEK.NBT.E. 1 Demonstrate how to compose 7 by matching 5 ones and 2 more ones.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics |
| :--- | :--- | :--- |
| Content Standards |$\quad$| 2020 Wyoming Math |
| :--- |
| Extended Standards | Instructional Achievement Level Descriptor (AL_Ds)

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

K.MD.G. 4 Identify U.S. coins by name (pennies, nickels, dimes, and quarters).

## 2018 Wyoming Mathematics Content Standards

## Geometry

Identify and describe shapes (squares, circles, triangles, rectangles, hexagons, cubes, cones, cylinders, and spheres). (H)
K.G.H. 1 Describe objects in the environment using names of shapes, and describe the relative positions of these objects using terms such as above, below, beside, in front of, behind, and next to.
K.G.H. 2 Correctly name shapes regardless of their orientations or overall size.
K.G.H. 3 Identify shapes as twodimensional or three-dimensional.

EEK.MD.G. 4 When given a U.S. coin name, identify the correct coin (penny and quarter).

## 2020 Wyoming Math

 Extended Standards
## Grade K

EEK.G.H. 1 Identify shapes (square, triangle, rectangle, and circle) and describe their positions in relation to another object in the environment using the terms (in, out, over, under).

EEK.G.H.2-3 Correctly identify 4 shapes (circle, square, rectangle, and triangle).

Level IV AA Students will:
EEK.MD.G. 4 When given a U.S. coin name, identify 3 of 4 coins correctly. (e.g., penny, nickel, dime, or quarter).
Level III AA Students will:
EEK.MD.G. 4 When given a U.S. coin name, identify the correct coin (penny and quarter).
Level II AA Students will:
EEK.MD.G. 4 When given a U.S. coin name identify the correct coin (penny or quarter).
Level I AA Students will:
EEK.MD.G. 4 Match a U.S. coin with the same coin (penny/penny or quarter/quarter).

Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EEK.G.H. 1 Identify shapes and describe their positions in relation to another object in the environment using the terms (in, out, over, under, on, and beside).
Level III AA Students will:
EEK.G.H. 1 Identify shapes (square, triangle, rectangle, and circle) and describe their positions in relation to another object in the environment using the terms (in, out, over, under).
Level II AA Students will:
EEK.G.H. 1 Imitate a teacher model of two shapes and their relative position.
Level I AA Students will:
EEK.G.H. 1 Imitate a teacher model of one shape and its relative position.
Level IV AA Students will:
EEK.G.H.2-3 Correctly identify 4 two-dimensional shapes (circle, square, rectangle, and triangle) and 1 three-dimensional shape (cube, sphere, cylinder, cone). Level III AA Students will:
EEK.G.H.2-3 Correctly identify 4 shapes (circle, square, rectangle, and triangle).
Level II AA Students will:
EEK.G.H.2-3 Correctly identify 2 out of 4 shapes (circle, square, rectangle, or triangle).
Level I AA Students will:
EEK.G.H.2-3 Correctly match 2 out of 4 shapes (circle, square, rectangle, or triangle).

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Analyze, compare, create, and
compose shapes. (I)
K.G.I. 4 Analyze and compare twoand three-dimensional shapes, using informal language to describe their similarities, differences, and attributes.
K.G.I. 5 Model shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.
K.G.I. 6 Use simple shapes to compose squares, rectangles, and hexagons.

EEK.G.I. 4 Sort two- and three-dimensional shapes.

EEK.G.I. 5 Model at least 2 different simple shapes by building simple shapes from components.

EEK.G.I. 6 Use 2-4 equally shaped parts to compose squares and rectangles with a template.

Level IV AA Students will:
EEK.G.I. 4 Sort two- and three-dimensional shapes to describe similarities (square/cube and circle/sphere).
Level III AA Students will:
EEK.G.I. 4 Sort two- and three-dimensional shapes.
Level II AA Students will:
EEK.G.I. 4 Sort two-dimensional shapes.
Level I AA Students will:
EEK.G.I. 4 Match similar 2 two-dimensional shapes to each other.
Level IV AA Students will:
EEK.G.I. 5 Model or draw 2 or more different simple shapes by building or drawing simple shapes from components.
Level III AA Students will:
EEK.G.I. 5 Model at least 2 different simple shapes by building simple shapes from components.
Level II AA Students will:
EEK.G.I. 5 Modei a simple shape by building a simple shape.
Level I AA Students will:
EEK.G.I. 5 Match simple shapes to each other.
Level IV AA Students will:
EEK.G.1. 6 Use 2-4 equally shaped parts to compose squares or rectangles without a template.
Level III AA Students will:
EEK.G.I. 6 Use 2-4 equally shaped parts to compose squares and rectangles with a template.
Level II AA Students will:
EEK.G.I. 6 Use simple shapes to compose a square or a rectangle using a template.
Level I AA Students will:
EEK.G.I. 6 Use simple shapes to compose a square using a template.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content Standards

## Operations and Algebraic

 ThinkingRepresent and solve problems involving addition and subtraction. (A)
1.OA.A. 1 Use addition and subtraction within 20 to solve word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, by using objects, drawings, or equations with a symbol for the unknown number to represent the problem.
1.OA.A. 2 Solve word problems that call for the addition of three whole numbers whose sum is less than or equal to 20 , by using objects, drawings, or equations.

## Understand and apply

 properties of operations and the relationship between addition and subtraction. (B)1.OA.B. 3 Apply commutative and associative properties of addition as strategies to add and subtract.
1.OA.B. 4 Understand subtraction as an unknown-addend problem.

2020 Wyoming Math Extended Standards

## Grade 1

EE1.OA.A. 1 When solving problems with sums up to 7 , students will use math strategies of "putting together" and "taking from/taking apart."

## EE1.OA.A. 2 Solve

 addition word problems with sums to 10EE1.OA.B. 3 Use the commutative property of addition to solve for a missing addend.

## EE1.OA.B. 4 Not

applicable; skill is covered in other standards.

Instructional Achievement Level Descriptor (ALDs)

## Level IV AA Students will:

EE1.OA.A. 1 When solving problems with sums up to 10, students will use math strategies of "putting together" and "taking from/taking apart."
Level III AA Students will:
EE1.OA.A.1 When solving problems with sums up to 7, students will use math strategies of "putting together" and "taking from/taking apart."
Level II AA Students will:
EE1.OA.A. 1 When solving problems with sums up to 5 , students will use math strategies of "putting together."
Level I AA Students will:
EE1.OA.A. 1 When solving problems with sums up to 3 , students will use math strategies of "putting together."
Level IV AA Students will:
EE1.OA.A. 2 Solve addition word problems with sums to 10 using 3 whole numbers.
Level III AA Students will:
EE1.OA.A. 2 Solve addition word problems with sums to 10 .
Level II AA Students will:
EE1.OA.A. 2 Solve addition word problems with sums to 7 .
Level I AA Students will:
EE1.OA.A. 2 Solve an addition problems with a sum to 5 .

## Level IV AA Students will:

EE1.OA.B. 3 Apply the commutative and associative properties to solve addition problems for missing addends. Level III AA Students will:
EE1.OA.B. 3 Use the commutative property of addition to solve for a missing addend. Level II AA Students will:
EE1.OA.B. 3 Demonstrate the commutative property of addition when given a set of 2 numbers.
Level I AA Students will:
EE1.OA.B. 3 Match the commutative property of addition.
***The Extended Standards Educator Committee determined there are no realworld applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Add and subtract within 20. (C)
1.OA.C. 5 Relate counting to addition and subtraction using strategies, such as, by counting on and back.
1.OA.C. 6 Add and subtract within

20, demonstrating fluency in addition and subtraction within 10 . Use strategies such as counting on; making ten using the relationship between addition and subtraction.

Work with addition and subtraction equations. (D)
1.OA.D. 7 Understand the meaning of the equal sign, and determine if equations involving addition and subtraction are true or false.
1.OA.D. 8 Determine the unknown whole number in an addition or subtraction equation relating three whole numbers.

EE1.OA.C. 5 Use
"counting on" and "counting back" when solving addition and subtraction problems with numbers to 10.

EE1.OA.C. 6 Fluently add within 10.

## EE1.OA.D. 7

Understand the meaning of the equal sign involving addition equations with sums of 10.

EE1.OA.D. 8 Determine the unknown whole number in an addition equation relating 3 whole numbers to 10 .

Level IV AA Students will:
EE1.OA.C. 5 Use "counting on" and "counting back" when solving addition and subtraction problems with numbers to 20.

## Level III AA Students will:

EE1.OA.C. 5 Use "counting on" and "counting back" when solving addition and subtraction problems with numbers to 10.
Level II AA Students will:
EE1.OA.C. 5 Use "counting back" when solving subtraction problems with numbers to 5.

Level I AA Students will:
EE1.OA.C. 5 Use "counting on" when solving addition problems with numbers to 5 .
Level IV AA Students will:
EE1.OA.C. 6 Fluently add and subtract within 10.
Level III AA Students will:
EE1.OA.C. 6 Fluently add within 10.
Level II AA Students will:
EE1.OA.C. 6 Fluently add within 5.

## Level I AA Students will:

EE1.OA.C. 6 Fluently add within 3.
Level IV AA Students will:
EE1.OA.D. 7 Understand the meaning of the equal sign involving addition and subtraction equations with sums/differences to 20.
Level III AA Students will:
EE1.OA.D. 7 Understand the meaning of the equal sign involving addition equations with sums of 10.
Level II AA Students will:
EE1.OA.D. 7 Understand the meaning of the equal sign involving groups of no more than 5 objects.

## Level I AA Students will:

EE1.OA.D. 7 Match equal groups using no more than 5 objects in each group.
Level IV AA Students will:
EE1.OA.D. 8 Determine the unknown whole number in addition and subtraction equations relating 3 whole numbers to 10.
Level III AA Students will:
EE1.OA.D. 8 Determine the unknown whole number in an addition equation relating 3 whole numbers to 10.
Level II AA Students will:
EE1.OA.D. 8 Determine the unknown whole number in an addition equation relating 3 whole numbers to 5 .
Level I AA Students will:

DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

|  |  | EE1.OA.D. 8 Determine the unknown whole number in an addition equation relating 3 whole numbers to 3 . |
| :---: | :---: | :---: |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Number and Operations Base Ten | Grade 1 |  |
| Extend the counting sequence. (E) <br> 1.NBT.E. 1 Extend the number sequences to 120 . In this range: <br> A. Count forward and backward, starting at any number less than 120. <br> B. Read numerals. <br> C. Write numerals. <br> D. Represent a number of objects with a written numeral. | EE1.NBT.E.1a Starting at a given number, other than 1, count forward by ones to 20 . <br> EE1.NBT.E.1b Count backwards from 20. <br> EE1.NBT.E.1c Identify numbers 1-20. <br> EE1.NBT.E.1d Count a number of objects then match with a numerical symbol 1-20. | Level IV AA Students will: <br> EE1.NBT.E.1a Starting at a given number other than 1, count forward by ones to 30 . <br> EE1.NBT.E.1b Count backwards from 20 <br> EE1.NBT.E.1c Identify and write numbers 1-30. <br> EE1.NBT.E.1d Count a numbe of objects then match with a numerical symbol 1-30. <br> Level III AA Students will: <br> EE1.NBT.E.1a Starting at a given number, other than 1, count forward by ones to 20. <br> EE1.NBT.E.1b Count backwards from 10. <br> EE1.NBT.E.1c Identify numbers 1-20. <br> EE1.NBT.E.1d Count a number of objects then match with a numerical symbol 1-20. <br> Level II AA Students will: <br> EE1.NBT.E.1a Starting at a given number, other than 1, count forward by ones to 10. <br> EE1.NBT.E.1b Count backwards from 5. <br> EE1.NBT E.1c Identify numbers 1-10. <br> EE1.NBTE.1d Count a number of objects then match with a numerical symbol 1-10. <br> Level I AA Students will: <br> EE1.NBT.E.1a Count forward by ones to 5 . <br> EE1.NBT.E.1b Count backwards from 3. <br> EE1.NBT.E.1c Match numbers 1-10. <br> EE1.NBT.E.1d Count a number of objects then match with a numerical symbol 1-5. |
| Understand place value. (F) <br> 1.NBT.F. 2 Understand that the two digits of a two-digit number represent amounts of tens and ones. Understand the following as special cases: <br> A. 10 can be thought of as a bundle of ten ones - called a "ten." <br> B. The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight or nine ones. | EE1.NBT.F. 2 Given a multiple of 10, create bundles of ten to represent that number. | Level IV AA Students will: <br> EE1.NBT.F. 2 Compose numbers from 11-19 by using a set of ten and more ones, or create $20,30,40$, or 50 using sets of ten. <br> Level III AA Students will: <br> EE1.NBT.F. 2 Given a multiple of 10, create bundles of ten to represent that number. <br> Level II AA Students will: <br> EE1.NBT.F. 2 Create one set of 10. <br> Level I AA Students will: <br> EE1.NBT.F. 2 Match a given set of 10 to another set of 10 . |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| C. The numbers $10,20,30,40$, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones). |  |  |
| :---: | :---: | :---: |
| 1.NBT.F. 3 Compare pairs of twodigit numbers based on the values of the tens digit and the ones digits, recording the results of comparisons with the words "is greater than," "is equal to," "is less than," and with the symbols >, $=$, and $<$. | EE1NBT.F. 3 Compare two groups of items (10 or fewer) using the terms "greater than" and "less than." | Level IV AA Students will: <br> EE1NBT.F. 3 Compare two groups of items (10 or fewer) using the terms <br> "greater than," "less than," and "equal to.' <br> Level III AA Students will: <br> EE1NBT.F. 3 Compare two groups of items (10 or fewer) using the terms "greater than" and "less than." <br> Level II AA Students will: <br> EE1NBT.F. 3 Compare two groups of items (10 or fewer) using the terms "greater than" or "less than." <br> Level I AA Students will: <br> EE1NBT.F. 3 Given a group of 2 objects and 6 objects, identify which group is "greater than." |
| Use place value understanding and properties of operations to add and subtract. (G) <br> 1.NBT.G. 4 Add within 100, using concrete models or drawings and strategies based on place value: <br> A. Including adding a two-digit number and a one-digit number. <br> B. Adding a two-digit number and a multiple of 10 . <br> C. Understand that in adding two-digit numbers, add tens and tens, ones and ones; and sometimes it is necessary to compose a ten. <br> D. Relate the strategy to a written method and explain the reasoning used. | EE1.NBT.G. 4 Add within 15 using models or manipulatives based on "place value" and using one digit and two digit numbers. | Level IV AA Students will: <br> EE1.NBT.G.4 Add within 20 using models or manipulatives based on "place value" and using one digit and two digit numbers. <br> Level III AA Students will: <br> EE1.NBT G.4 Add within 15 using models or manipulatives based on "place value" and using one digit and two digit numbers. <br> Level II AA Students will: <br> EE1.NBT.G. 4 Identify the number(s) in the tens and ones places in an addition problem whose sum is greater than 10 but less than 15. <br> Level I AA Students will: <br> EE1.NBT.G. 4 Given a 2 digit number between 10 and 15, identify the tens and ones places. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

1.NBT.G. 5 Given a two-digit
number, mentally find 10 more or 10 less than the number, without having a count; explain the reasoning used.

EE1.NBT.G. 5 Given the number 20 find "ten more" and "ten less" than the number.

## 2018 Wyoming Mathematics Content Standards

## Measurement and Data

Measure lengths indirectly and by iterating length units. (H) 1.MD.H. 1 Order three objects by length; compare the lengths of two objects indirectly by using a third object.

## 2020 Wyoming Math Extended Standards

## Grade 1

EE1.MD.H. 1 When presented with 3 objects, order those objects by length.

Level IV AA Students will:
EE1.NBT.G. 5 Given the number 30 find "ten more" and "ten less" than the number. Level III AA Students will:
EE1.NBT.G. 5 Given the number 20 find "ten more" and "ten less" than the number.
Level II AA Students will:
EE1.NBT.G. 5 Given the number 20, show "ten more" than the number.
Level I AA Students will:
EE1.NBT.G. 5 Match the numbers 10, 20, 30 to the correct corresponding value.
Level IV AA Students will:
EE1.NBT.G. 6 Subtract multiples of 10 from a larger multiple of ten no greater than 40 using models or manipulatives based on place value.
Level III AA Students will:
EE1.NBT.G. 6 Subtract multiples of 10 from a larger multiple of ten no greater than 30 using models or manipulatives based on place value.
Level II AA Students will:
EE1.NBT.G. 6 Subtract multiples of 10 from a larger multiple of ten no greater than 20 using models or manipulatives based on place value.
Level I AA Students will:
EE1.NBT,G.6 Match the numbers 30, 20, 10 to the correct corresponding value in reverse sequence.

## Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EE1.MD.H. 1 Order two objects by length; compare the lengths of those objects indirectly by using a third object.

## Level III AA Students will:

EE1.MD.H. 1 When presented with 3 objects, order those objects by length.

## Level II AA Students will:

EE1.MD.H. 1 When presented with 2 objects, order those objects by length.
Level I AA Students will:
EE1.MD.H. 1 Match different sized objects.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

1.MD.H. 2 Use nonstandard units to show the length of an object as the number of same size units of length with no gaps or overlaps.

## Tell and write time. (I)

1.MD.I. 3
A. Tell and write time in hours and half-hours using analog and digital clocks.
B. Identify U.S. coins by value (pennies, nickels, dimes, quarters)

## Represent and interpret data.

(J)
1.MD.J. 4 Organize, represent, and interpret data with up to three categories; ask and answer questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.

EE1.MD.H. 2 Use nonstandard units to show the length of an object.

Level IV AA Students will:
EE1.MD.H. 2 Use 2 different nonstandard units to show the length of an object.
Level III AA Students will:
EE1.MD.H. 2 Use nonstandard units to show the length of an object.
Level II AA Students will:
EE1.MD.H. 2 Complete the measure of a model using the given nonstandard units.
Level I AA Students will:
EE1.MD.H. 2 Match the nonstandard units used to measure an object.
Level IV AA Students will:
EE1.MD.I.3a Tell time in hours using a digital clock and an analog clock.
EE1.MD.I.3b Identify 3 out of 4 U.S. coins and their values (pennies, nickels, dimes, quarters).

## Level III AA Students will:

EE1.MD.I.3a Tell time in hours using a digital clock.
EE1.MD.I.3b Identify 2 out of 4 U.S. coins and their values (pennies, nickels, dimes, quarters).
Level II AA Students will:
EE1.MD.I.3a Match hour and half-hour times on a digital clock.
EE1.MD.I.3b Sort U.S. coins according to value.
Level I AA Students will:
EE1.MD I.3a Match hour times on a digital clock.
EE1.MD.I.3b Match U.S. coin with a given U.S. coin.
Level IV AA Students will:
EE1.MD.J. 4 Interpret data in two categories: identify how many in each category and determine whether there are more or less in each category.
Level III AA Students will:
EE1.MD.J. 4 Interpret data in two categories to determine whether there are more or less in each category.
Level II AA Students will:
EE1.MD.J. 4 Interpret data in two categories to determine which category has more. Level I AA Students will:
EE1.MD.J. 4 Match a number of objects to data provided on a simple graph.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics |
| :--- | :--- | :--- |
| Content Standlards |$\quad$| 2020 Wyoming Math |
| :--- |
| Extended Standards | Instructional Achievement Level Descriptor (AL.Ds)

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content Standards
Operations and Algebraic Thinking
Represent and solve problems involving addition and subtraction. (A)
2.OA.A. 1 Use addition and subtraction within 100 to solve oneand two-step word problems involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, by using drawings and equations with a symbol for the unknown number to represent the problem.

Add and subtract within 20. (B)
2.OA.B. 2 Fluently add and subtract within 20 using mental strategies. By end of Grade 2, know automatically all sums of two one-digit numbers based on strategies.

Work with equal groups of objects to gain foundations for multiplication. (C)
2.OA.C. 3 Determine whether a group (up to 20) has an odd or even number of objects (e.g., by pairing objects or counting them by 2 s ).
A. If the number of objects is even, then write an equation to express this as the sum of two equal addends.
B. If the number of objects group is odd, then write an equation to express this as a

2020 Wyoming Math Extended Standards

## Grade 2

## EE2.OA.A. 1 Use

addition and subtraction within 30 to solve problems involving situations of adding to, taking from, putting together, and taking apart.

## EE2.OA.B. 2 Fluently

 add to 20 and subtract within 10.
## EE2.OA.C. 3 Determine

 whether a group (up to 20) has an odd or even number of objects (e.g., by pairing objects or counting them by 2 s ).Instructional Achievement Level Descriptor (AL.DS)

## Level IV AA Students will:

EE2.OA.A. 1 Use addition and subtraction within 40 to solve word problems involving situations of adding to, taking from, putting together, and taking apart.

## Level III AA Students will:

EE2.OA.A. 1 Use addition and subtraction within 30 to solve word problems involving situations of adding to, taking from, putting together, and taking apart. Level II AA Students will:
EE2.OA.A.1 Use addition within 20 to solve word problems involving situations of adding to and putting together.
Level I AA Students will:
EE2.OA.A. 1 Use addition within 10 to solve word problems.

Level IV AA Students will:
EE2.OA.B.2 Fluently add to 20 and subtract within 20.
Level îl AA Students will:
EE2.OA.B. 2 Fluently add to 20 and subtract within 10.
Level II AA Students will:
EE2.OA.B. 2 Fluently add to 10 and subtract within 5.
Level I AA Students will:
EE2.OA.B. 2 Fluently add to 5 and subtract within 3.
Level IV AA Students will:
EE2.OA.C. 3 Determine whether a group (up to 20) has an odd or even number of objects (e.g., by pairing objects or counting them by 2 s ) and make an addition equation using objects (up to 10).
Level III AA Students will:
EE2.OA.C. 3 Determine whether a group (up to 20) has an odd or even number of objects (e.g., by pairing objects or counting them by 2 s ).
Level II AA Students will:
EE2.OA.C. 3 Match objects by pairs of two using a template and determine if a group of objects is odd or even in number.
Level I AA Students will:
EE2.OA.C. 3 Match objects by pairs of two using a template.

DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| sum of a near double (double plus 1). |  |  |
| :---: | :---: | :---: |
| 2.OA.C. 4 Use addition to find the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; write an equation to express the total as a sum of equal addends. | EE2.OA.C. 4 Use <br> addition to find the total number of objects arranged within 3 rows and 3 columns. | Level IV AA Students will: <br> EE2.OA.C. 4 Use addition to find the total number of objects arranged within 3 rows and 3 columns then make an equation to express the total as a sum of equal addends. <br> Level III AA Students will: <br> EE2.OA.C. 4 Use addition to find the total number of objects arranged within 3 rows and 3 columns. <br> Level II AA Students will: <br> EE2.OA.C. 4 Use addition to find the total number of objects arranged within 3 rows and 3 columns with a template. <br> Level I AA Students will: <br> EE2.OA.C. 4 Create equal groups of objects (up to 3). |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Number and Operations Base Ten | Grade 2 |  |
| Understand place value. (D) 2.NBT.D. 1 Understand that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; and demonstrate that: <br> A. 100 can be thought of as a bundle of ten tens - called a "hundred." <br> B. The numbers $100,200,300$, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones). <br> C. Three-digit numbers can be decomposed in multiple ways (e.g., 524 can be decomposed as 5 hundreds, 2 tens and 4 ones or 4 | EE2.NBT.D. 1 Identify the digits in the one and tens place to 99 . Demonstrate that 100 can be thought of as a bundle of 10 tens called a "hundred." | Level IV AA Students will: <br> EE2.NBT.D. 1 Understand that bundles of two-digit objects represent ones and tens (from 50-99). Demonstrate that: <br> - 100 can be thought of as a bundle of 10 tens - called a "hundred" <br> - The numbers $100,200,300,400$, or 500 can be thought of as bundles of 100 <br> Level III AA Students will: <br> EE2.NBT.D. 1 Identify the digits in the one and tens place to 99. Demonstrate that 100 can be thought of as a bundle of 10 tens - called a "hundred." <br> Level II AA Students will: <br> EE2.NBT.D. 1 Match given digits to the correct ones and tens place to 50. Complete a model using bundles of 10 to show $50,60,70,80,90$, and 100. <br> Level I AA Students will: <br> EE2.NBT.D. 1 Match bundles of ten to show 50. |

DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| hundreds, 12 tens, and 4 ones, etc.) |  |  |
| :---: | :---: | :---: |
| 2.NBT.D. 2 Skip-count by 10s and 100s within 1000 starting at any given number. | EE2.NBT.D. 2 Count by tens to 100. | Level IV AA Students will: <br> EE2.NBT.D. 2 Count by tens to 150 or count by hundreds to 500 . <br> Level III AA Students will: <br> EE2.NBT.D. 2 Count by tens to 100 . <br> Level II AA Students will: <br> EE2.NBT.D. 2 Count by tens to 50 . <br> Level I AA Students will: <br> EE2.NBT.D. 2 Count by tens to 20. |
| 2.NBT.D. 3 Read and write numbers to 1000 using base-ten numerals, number names, and expanded form. | EE2.NBT.D. 3 Identify numbers to 50 . | Level IV AA Students will? <br> EE2.NBT.D. 3 Identify or write numbers to 100. <br> Level III AA Students will: <br> EE2.NBT.D. 3 Identify numbers to 50. <br> Level II AA Students will: <br> EE2.NBT.D. 3 Identify numbers to 30. <br> Level I AA Students will: <br> EE2.NBT.D. 3 Identify numbers to 10. |
| 2.NBT.D. 4 Compare pairs of threedigit numbers based on meanings of the hundreds, tens, and ones digits, using the words "is greater than," "is equal to," "is less than" and with the symbols >, =, and < to record the results of comparisons. | EE2.NBT.D. 4 Compare sets of objects or numbers (up to 50) using appropriate vocabulary ("greater/more than," "less than," "equal to"). | Level IV AA Students will: <br> EE2.NBT.D. 4 Compare numbers (up to 100) using appropriate vocabulary ("greater/more than," "less than," "equal to") and the symbols ">", "<", "=". <br> Level III AA Students will: <br> EE2.NBT.D. 4 Compare sets of objects or numbers (up to 50) using appropriate vocabulary ("greater/more than," "less than," "equal to"). <br> Level II AA Students will: <br> EE2.NBT.D. 4 Compare sets of objects or numbers (up to 30) using appropriate vocabulary ("greater/more than," "less than," "equal to"). <br> Level I AA Students will: <br> EE2.NBT.D. 4 Compare sets of objects or numbers (up to 15) using appropriate vocabulary ("greater/more than" or "less than"). |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Use place value understanding and properties of operations to add and subtract. (E)
2.NBT.E. 5 Add and subtract within 100 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction.
2.NBT.E. 6 Add up to four two-digit numbers using strategies based on place value and/or properties of addition.
2.NBT.E. 7 Add and subtract within 1000, using concrete models or drawings and strategies based on place value, properties of addition, and/or the relationship between addition and subtraction:
A. Relate the strategy to a written method and explain the reasoning used.
B. Understand that in adding on subtracting three-digit numbers, add or subtract hundreds and hundreds, tens and tens, ones and ones.

EE2.NBT.E. 5 Add and subtract within 30 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction

EE2.NBT.E. 6 Add 2
two-digit numbers (1050) using strategies based on place value and/or properties of addition.

Level IV AA Students will:
EE2.NBT.E. 5 Add and subtract within 50 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction. Level III AA Students will:
EE2.NBT.E.5 Add and subtract within 30 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction. Level II Students will:
EE2.NBT.E. 5 Add and subtract within 20 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction. Level I AA Students will
EE2.NBT.E. 5 Add and subtract within 10 using strategies based on place value, properties of addition, and/or the relationship between addition and subtraction.

## Level IV AA Students will:

EE2.NBT.E. 6 Add 2 two-digit numbers (50-90) using strategies based on place value and/or properties of addition.
Level III AA Students will:
EE2.NBT.E.6 Add 2 two-digit numbers (10-50) using strategies based on place value and/or properties of addition.
Level II AA Students will:
EE2.NBT.E. 6 Add a one digit (1-9) and a two-digit number (10-20) using strategies based on place value and/or properties of addition.
Level I AA Students will:
EE2.NBT.E. 6 Add 2 one digit numbers (1-9) using strategies based on place value and/or properties of addition.

Level IV AA Students will:
EE2.NBT.E. 7 Add and subtract within 300, using concrete models, manipulatives, or drawings and strategies based on place value, or properties of addition.

## Level III AA Students will:

EE2.NBT.E. 7 Add and subtract within 100, using concrete models, manipulatives, or drawings and strategies based on place value, or properties of addition.

## Level II AA Students will:

EE2.NBT.E. 7 Add and subtract within 50, using concrete models, manipulatives, or drawings and strategies based on place value, or properties of addition.
Level I AA Students will:
EE2.NBT.E. 7 Add and subtract within 30 , using concrete models, manipulatives, or drawings and strategies based on place value, or properties of addition.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS



## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2.MD.F. 2 Measure the same object or distance using a standard unit of one length and then a standard unit of a different length. Explain how the two measurements relate to the size of the unit chosen.
2.MD.F. 3 Estimate lengths using units of inches, feet, centimeters, and meters.
2.MD.F. 4 Measure in standard length units to determine how much longer one object is than another.

## Relate addition and subtraction

to length. (G)
2.MD.G. 5 Use addition and subtraction within 100 to solve word problems involving lengths that are given in the same units.
2.MD.G. 6 Use a number line diagram with equally spaced points to:
A. Represent whole-number sums and differences within 100 on a number line diagram.

EE2.MD.F. 2 Measure one object or distance to the nearest whole unit of length using 2 standard units (e.g., inches, feet).

EE2.MD.F.3-4 Given an object, determine the unit of measurement as inches or feet.

Level IV AA Students will:
EE2.MD.F. 2 Measure multiple objects or distances using 2 standard units (e.g., inches, feet) to the nearest whole unit.

## Level III AA Students will:

EE2.MD.F. 2 Measure one object or distance to the nearest whole unit of length using 2 standard units (e.g., inches, feet).
Level II AA Students will:
EE2.MD.F. 2 Measure one object to the nearest whole using a ruler (inches).
Level I AA Students will:
EE2.MD.F. 2 Identify a ruler.

## Level IV AA Students will:

EE2.MD.F.3-4 Estimate the length of multiple objects using inches or feet. Level III AA Students will:
EE2.MD.F.3-4 Given an object, determine the unit of measurement as inches or feet. Level II AA Students will:
EE2.MD.F.3-4 Given 3 objects, place objects in order by length from shortest to longest.
Level I AA Students will:
EE2.MD.F.3-4 Given 3 objects, identify which is longest.

## Level IV AA Students will:

EE2.MD.G. 5 Use subtraction to solve one-step word problems using lengths that are in the same units.

## Level III AA Students will:

EE2.MD.G. 5 Use addition to solve one-step word problems using lengths that are in the same units.
Level II AA Students will:

## EE2.MD.G. 5

Use addition to solve one-step word problems by adding a single unit to increase length.
Level I AA Students will:
EE2.MD.G. 5 Increase length by adding a single unit.

## Level IV AA Students will:

EE2.MD.G. 6 Use a number line diagram with equally spaced points to locate the multiple of 10 before and after a given number within 100.
Level III AA Students will:
EE2.MD.G. 6 Use a number line diagram with equally spaced points to locate the multiple of 10 before or after a given number within 100

Wyoming Department of Education edu.wyoming.gov/standards

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| B. Locate the multiple of 10 before and after a given number within 100. | after a given number within 100. | Level II AA Students will: <br> EE2.MD.G. 6 Use a number line to count backwards by tens from 100. <br> Level I AA Students will: <br> EE2.MD.G. 6 Use a number line to count backwards by ones from 10. |
| :---: | :---: | :---: |
| Work with time and money. (H) 2.MD.H. 7 Tell and write time from analog and digital clocks in five minute increments using a.m. and p.m. | EE2.MD.H. 7 Tell or write time to the hour using an analog clock or digital clock. | Level IV AA Students will: <br> EE2.MD.H. 7 Tell or write time to the half-hour using an analog clock or digital clock. <br> Level III AA Students will: <br> EE2.MD.H. 7 Tell or write time to the hour using an analog clock or digital clock. <br> Level II AA Students will: <br> EE2.MD.H. 7 Identify which digit(s) or hand marks the hour on a clock. <br> Level I AA Students will: <br> EE2.MD.H. 7 Identify a measurement tool that tells time. |
| 2.MD.H. 8 Solve word problems up to $\$ 10$ involving dollar bills, quarters, dimes, nickels, and pennies, using \$ (dollars) and $\Phi$ (cents) symbols appropriately. | EE2.MD.H. 8 Solve word problems up to \$1, involving pennies and dimes, using the cents ( $\Phi$ ) symbol. | Level IV AA Students will: <br> EE2.MD.H. 8 Solve word problems up to $\$ 1$ involving pennies, nickels, dimes, and quarters using the $\mathbb{C}$ (cents) symbol. <br> Level III AA Students will: <br> EE2.MD.H. 8 Solve word problems up to $\$ 1$, involving pennies and dimes, using the $\Phi$ (cents) symbol. <br> Level II AA Students will: <br> EE2.MD.H. 8 Identify the values of coins (pennies, nickels, dimes, quarters) and <br> identify the $\Phi$ (cents) symbol. <br> Level I AA Students will: <br> EE2.MD.H. 8 Identify coins (pennies, nickels, dimes, quarters). |
| Represent and interpret data. <br> (I) <br> 2.MD.I. 9 Generate measurement data based on whole units and show data by making a line plot. | EE2.MD.I. 9 Place 7 given data points on a template to complete a line plot. | Level IV AA Students will: <br> EE2.MD.I. 9 When given 3 measurement data, create a line plot. <br> Level III AA Students will: <br> EE2.MD.I. 9 Place 7 given data points on a template to complete a line plot. <br> Level II AA Students will: <br> EE2.MD.I. 9 Place 3 given data points on a template to complete a line plot. <br> Level I AA Students will: <br> EE2.MD.I. 9 Identify a line plot from 3 pictures. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2.MD.I. 10 Use data to:
A. Draw a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories.
B. Solve simple put-together, take-apart, and compare problems using information presented in a bar graph.

## 2018 Wyoming Mathematics

 Content Standards
## Geometry

Reason with shapes and their attributes.
2.G.J. 1 Identify triangles,
quadrilaterals, pentagons, hexagons, and cubes. Recognize and draw shapes having specified attributes, such as a given number of angles or a given number of equal faces. (Sizes are compared directly or visually, not compared by measuring.)
2.G.J. 2 Partition a rectangle into rows and columns of same-size squares and count to find the total number of them.

EE2.MD.I. 10 Place
given objects (data) on to a template to complete picture graph.

Level IV AA Students will:
EE2.MD.I. 10 Use data to draw or create a picture graph or a bar graph to represent a data set.
Level III AA Students will:
EE2.MD.I. 10 Place given objects (data) on to a template to complete picture graph. Level II AA Students will:
EE2.MD.I. 10 Match objects (data) on a completed picture or bar graph.
Level I AA Students will:
EE2.MD.I. 10 Identify a picture and bar graph from a group of 3 pictures.
Instructional Achievement Level Descriptor (ALDs)

## Grade 2

EE2.G.J. 1 Identify triangles, squares, pentagons, octagons. Recognize and create shapes having specified attributes.

## EE2.G.J. 2 Given a

 partitioned rectangle, count the number of same-sized squares.
## Level IV AA Students will:

EE2.G.J. 1 Identify triangles, squares, pentagons, octagons. Recognize and create shapes having specified attributes. Identify the number of angles in a given shape. Level III AA Students will:
EE2.G.J. 1 Identify triangles, squares, pentagons, octagons. Recognize and create shapes having specified attributes. Level II AA Students will:
EE2.G.J. 1 Identify 3 shapes (triangles, squares, pentagons, octagons). Recognize or create shapes having specified attributes.
Level I AA Students will:
EE2.G.J. 1 Match shapes (triangles, squares, pentagons, octagons) to each other.

## Level IV AA Students will:

EE2.G.J. 2 Given a partitioned rectangle, count the number of same-sized squares, columns, and rows.
Level III AA Students will:
EE2.G.J. 2 Given a partitioned rectangle, count the number of same-sized squares. Level II AA Students will:
EE2.G.J. 2 Given a partitioned rectangle, place same-sized squares to complete the interior of the figure.

## Level I AA Students will:

EE2.G.J. 2 Given a partitioned rectangle, match the same-sized squares to the interior of the figure.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2.G.J. 3 Partition circles and rectangles into two, three, or four equal shares by:
A. Describing the shares using the words halves, thirds, half of, a third of, etc.
B. Describing the whole as two halves, three thirds, four fourths.
C. Recognizing that equal shares of identical wholes need not have the same shape.

EE2.G.J. 3 Partition circles and rectangles into two and four equal shares.

Level IV AA Students will:
EE2.G.J.3 Partition circles and rectangles into two, three, and four equal shares. Describe the shares using the words halves, thirds, and fourths.
Level III AA Students will:
EE2.G.J.3 Partition circles and rectangles into two and four equal shares.
Level II AA Students will:
EE2.G.J. 3 Partition circles and rectangles into two or four equal shares.
Level I AA Students will:
EE2.G.J. 3 Match 2 or 4 pieces to make a circle or a rectangle.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics
Content Standards

## Operations and Algebraic

 ThinkingRepresent and solve problems involving multiplication and division. (A)
3.OA.A. 1 Represent the concept of multiplication of whole numbers using models including, but not limited to, equal-sized groups ("groups of"), arrays, area models, repeated addition, and equal "jumps" on a number line.
3.OA.A. 2 Represent the concept of division of whole numbers (resulting in whole number quotients) using models including, but not limited to, partitioning, repeated subtraction, sharing, and inverse of multiplication.
3.OA.A. 3 Solve multiplication and division word problems within 100 using appropriate modeling strategies and equations.
 number in a multiplication or division equation relating three whole numbers when the unknown is a missing factor,

## 2020 Wyoming Math

Extended Standards

## Grade 3

EE3.OA.A. 1 Identify appropriate models for multiplication of whole numbers (e.g., arrays, repeating addition, area models).

EE3.OA.A. 2 Identify appropriate models for division of whole numbers (e.g., arrays, repeating subtraction, area models).
given multiplication and division problems within 100 using appropriate modeling strategies.

EE3.OA.A. 4 Identify multiplication and division facts when

Instructional Achievement Level Descriptor (ALDS)

## Level IV AA Students will: <br> EE3.OA.A.1 Match a multiplication equation to an appropriate model.

Level III AA Students will:
EE3.OA.A. 1 Identify appropriate models for multiplication of whole numbers
(e.g., arrays, repeating addition, area models).

Level II AA Students will:
EE3.OA.A. 1 Combine equal groups to find the total whole number.
Level I AA Students will:
EE3.OA.A. 1 Identify equal groups of whole numbers with factors 1, 2, 5, 10.
Level IV AA Students will:
EE3.OA.A. 2 Match a division equation to an appropriate model.

## Level III AA Students will:

EE3.OA.A. 2 Identify appropriate models for division of whole numbers (e.g., arrays, repeating subtraction, area models).
Level II AA Students will:
EE3.OA.A. 2 Create equal groups from a given whole number with the divisor 2 and 5.
Level I AA Students will:
EE3.OA.A. 2 Identify equal groups of whole numbers with the divisor 2 and 5 .

## Level IV AA Students will:

## EE3.OA.A. 3

Solve a one-step multiplication or division word problem within 20.

## Level III AA Students will:

EE3.OA.A. 3 Solve given multiplication and division problems within 100 using appropriate modeling strategies.

## Level II AA Students will:

EE3.OA.A. 3 Solve given multiplication or division problems within 100 using appropriate modeling strategies.

## Level I AA Students will:

EE3.OA.A. 3 Identify an equation as multiplication or division problem.
Level IV AA Students will:
EE3.OA.A. 4 Find the unknown whole number in a multiplication or division equation when given a set of numbers.

Wyoming Department of Education

| product, dividend, divisor, or quotient. (Students need not know formal terms.) | given three whole correlating numbers. |
| :---: | :---: |
| Understand properties of multiplication and the relationship between multiplication and division. (B) 3.OA.B. 5 Apply properties of multiplication as strategies to multiply and divide. (Students need not use formal terms for these properties.) | EE3.OA.B. 5 Use an appropriate strategy to multiply or divide within 100. |
| 3.OA.B. 6 Understand division as an unknown-factor problem. | EE3.OA.B. 6 Not applicable. Benchmark is addressed in EE3.OA.B.2-5. |
| Multiply and divide within 100. (C) 3.OA.C. 7 Fluently multiply and divide with factors 1-10 using mental strategies. By end of Grade 3, know automatically all products of one-digit factors based on strategies. | EE3.OA.C. 7 Multiply and divide with factors 1-10 using strategies. |

## Level III AA Students will:

EE3.OA.A. 4 Identify multiplication and division facts when given three whole correlating numbers (i.e., given numbers $3,10,30$ : students will produce $3 \times 10=30,10 \times 3=30,30 / 3=10,30 / 10=3$ ).

## Level II AA Students will:

EE3.OA.A. 4 Identify multiplication or division facts when given three whole correlating numbers (i.e., given numbers $3,10,30$ : students will produce $3 \times 10=30,10 \times 3=30$, or, $30 / 3=10,30 / 10=3$ ).

## Level I AA Students will:

EE3.OA.A. 4 Solve multiplication and division problems with whole number factors 0-10.
Level IV AA Students will:
EE3.OA.B. 5 Use an appropriate strategy to multiply and divide within 100. Level III AA Students will:

EE3.OA.B. 5 Use an appropriate strategy to multiply or divide within 100.
Level II AA Stucents will:
EE3.OA.B. 5 Identify a strategy to multiply and divide within 100.

## Level I AA Students will:

EE3.OA.B. 5 Identify a strategy to multiply or divide within 100.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Level IV AA Students will:
EE3.OA.C. 7 Fluently multiply or divide with factors 1-10 using strategies.
Level III AA Students will:
EE3.OA.C. 7 Multiply and divide with factors 1-10 using strategies.
Level II AA Students will:
EE3.OA.C. 7 Multiply or divide with factors 1-10 using strategies.
Level I AA Students will:
EE3.OA.C. 7 Multiply or divide with factors 1-5 using strategies.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Solve problems involving the four operations, and identify and explain patterns in arithmetic. (D)
3.OA.D. 8 Solve two-step word problems (limited to the whole number system) using the four basic operations. Students should apply the Order of Operations when there are no parentheses to specify a particular order.
A. Represent these problems using equations with a symbol standing for the unknown quantity.
B. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.
3.OA.D. 9 Identify arithmetic patterns and explain the relationships using properties of operations.

EE3.OA.D. 8 Solve onestep addition/subtraction and multiplication/ division word problems by representation or using models.
*Committee chose not to address A or B; it is taught in 5th grade.

Level IV AA Students will:
EE3.OA.D. 8 Solve two step addition/subtraction or multiplication/division word problems by representation or using models.
Level III AA Students will:
EE3.OA.D. 8 Solve one step addition/subtraction and multiplication/division word problems by representation or using models.
Level II AA Students will:
EE3.OA.D. 8 Solve one step addition/subtraction or multiplication/division word problems by representation or using models.
Level I AA Students will:
EE3.OA.D. 8 Identify one step word problems as addition/subtraction.

EE3.OA.D. 9 Identify
arithmetic patterns in addition and multiplication.

Level IV AA Students will:
EE3.OA.D.9 Expand arithmetic patterns in addition and multiplication.
Level 11 AA Students will:
EE3.OA.D.9 Identify arithmetic patterns in addition and multiplication.
Level II AA Students will:
EE3.OA.D. 9 Expand an arithmetic pattern in addition or multiplication.
Level I AA Students will:
EE3.OA.D. 9 Identify an arithmetic pattern in addition or multiplication.
Instructional Achievement Level Descriptor (ALDs)

## Grade 3

EE3.NBT.E. 1
Recognize the value of the number in the ones and tens place. range of algorithms may be used). (E)
3.NBT.E. 1 Use place value understanding to round whole numbers to the nearest 10 or 100 .
3.NBT.E. 2 Fluently add and subtract within 1000 using strategies and

## Level IV AA Students will:

EE3.NBT.E. 1 When given one whole number, round to the nearest tens place.
Level III AA Students will:
EE3.NBT.E. 1 Recognize the value of the number in the ones and tens place.
Level II AA Students will:
EE3.NBT.E. 1 Identify if a number in the ones place is greater than, less than or equal to five.
Level I AA Students will:
EE3.NBT.E. 1 Identify the number in the ones and tens place.
Level IV AA Students will:
EE3.NBT.E. 2 Add and subtract from 51-100 using strategies or algorithms.

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3.NBT.E. 3 Multiply one-digit whole numbers by multiples of 10 in the range 10-90 (e.g., $9 \times 80,5 \times 60$ ) using strategies based on place value and properties of multiplication.
2018 Wyoming Mathematics

## Content Standards

Numbers and Operations -

## Fractions

## Develop understanding of

fractions as numbers. (F) (Limited
to denominators 2, 3, 4, 6, and 8)
*use horizontal fractions
3.NF.F. 1 Understand a fraction $1 / b$ as the quantity formed by 1 part when a whole is partitioned into $b$ equal parts; understand a fraction $a / b$ as the quantity formed by a parts of size $1 / b$.
3.NF.F. 2 Understand and represent fractions on a number line diagram.
A. Represent a fraction $1 / b$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into $b$ equal parts. Recognize that each part has size $1 / b$ and that the endpoint of the part based at 0 locates the number $1 / b$ on the number line.
B. Represent a fraction $a / b$ on a number line diagram by marking off a lengths $1 / b$ from
using strategies or algorithms.

EE3.NBT.E. 3 Match a given multiple of ten to a visual model.

## 2020 Wyoming Math

Extended Standards

## Grade 3

EE3.NF.F. 1 Create a whole using halves, thirds and fourths.

EE3.NF.F. 2 Identify
fractions with a
denominator of $2,3, \& 4$ on a number line.

Level III AA Students will:
EE3.NBT.E. 2 Add or subtract from 51-100 using strategies or algorithms.

## Level II AA Students will:

EE3.NBT.E. 2 Add and subtract within 50 using strategies or algorithms.
Level I AA Students will:
EE3.NBT.E. 2 Add or subtract within 50 using strategies or algorithms.
Level IV AA Students will:
EE3.NBT.E. 3 Multiply one digit whole numbers by 10.
Level III AA Students will:
EE3.NBT.E. 3 Match a given multiple of ten to a visual model.

## Level II AA Students will:

EE3.NBT.E. 3 Create groups of ten (e.g., manipulatives).
Level I AA Students wili:
EE3.NBT.E. 3 When given a visual model, show groups of ten.
Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EE3.NF.F. 1 Identify a given fractional part of a whole (i.e., $1 / 2,1 / 3,1 / 4$ ).
Level III AA Students will:
EE3.NF.F. 1 Create a whole using halves, thirds, and fourths.
Level il AA Students will:
EE3.NF.F. 3 Given a whole using halves, thirds, and fourths, identify how many equal parts.
Level I AA Students will:
EE3.NF.F. 1 Identify the whole.
Level IV AA Students will:
EE3.NF.F. 2 On an open number line place the fraction one-half and one-fourth.
Level III AA Students will:
EE3.NF.F. 2 Identify fractions with a denominator of 2, 3, 4 on a number line.
Level II AA Students will:
EE3.NF.F. 2 Identity 0,1 , and $1 / 2$ on the number line.

## Level I AA Students will:

EE3.NF.F. 2 Match fractions with their models on the number line.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 0. Recognize that the resulting interval has size $a / b$ and that its endpoint locates the number $a / b$ on the number line. |  |  |
| :---: | :---: | :---: |
| 3.NF.F. 3 Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size. <br> A. Understand two fractions as equivalent if they are the same size, or the same point on a number line. <br> B. Recognize and generate simple equivalent fractions. Explain why the fractions are equivalent. <br> C. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. <br> D. Compare two fractions with the same numerator or the same denominator, by reasoning about their size. Recognize that valid comparisons rely on the two fractions referring to the same whole. Record the results of comparisons with the symbols >, =, or <, and justify the conclusions. | EE3.NF.F. 3 Use a visual fraction model to compare fractions with denominators of $2,3, \&$ 4. | Level IV AA Students will: <br> EE3.NF.F. 3 Use a visual fraction model to compare fractions with denominators of $2,3, \& 4$. <br> Level III AA Students will: <br> EE3.NF.F. 3 Use a visual fraction model to identify fractions with denominators of $2,3, \& 4$. <br> Level II AA Students will: <br> EE3.NF.F. 3 Use a visual fraction model to compare one whole and one half. <br> Levell AA Students will: <br> EE3.NF.F. 3 Use a visual fraction model to identify one whole and one half. |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Measurement and Data | Grade 3 |  |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Solve problems involving measurement and estimation of intervals of time, liquid, volumes and masses of objects. (G)
3.MD.G. 1 Use analog clocks to tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes.
3.MD.G. 2 Measure and estimate liquid volumes and masses of objects using grams (g), kilograms (kg), and liters (L). (Excludes compound units such as $\mathrm{cm}^{3}$ and finding the geometric volume of a container.) Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units. (Excludes multiplicative comparison problems involving notions of "times as much.")
Represent and interpret data. (H) 3.MD.H. 3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled graphs.

EE3.MD.G. 1 Tell or
write time to the halfhour using an analog clock or digital clock.

EE3.MD.G. 2 Identify standard units of measure for mass and liquid using grams ( g ) and liters (L).
completed picture graph or bar graph to
less (e.g., colors weather, candy, shoes, height).

Level IV AA Students will:
EE3.MD.G. 1 Tell or write time from an analog or digital clock in five minute increments.

## Level III AA Students will:

EE3.MD.G. 1 Tell or write time to the half-hour using an analog clock or digital clock.
Level II AA Students will:
EE3.MD.G. 1 Using an analog or digital clock, tell time to the hour.
Level I AA Students will:
EE3.MD.G. 1 Identify which digit(s) or hand marks the half-hour on a clock.
Level IV AA Students will:
EE3.MD.G. 2 Add or subtract like units of measurement (i.e., grams ( g ) for mass and liters (L) for liquid)
Level III AA Students will:
EE3.MD.G. 2 Identify standard units of measure for mass and liquid using grams
( g ) and liters ( L )
Level II AA Students will:
EE3.MD.G. 2 Seiect the appropriate tool to measure a solid or a liquid.
Level IAA Students will:
EE3.MD.G. 2 Match a liquid to the correct measurement unit (i.e., liter).
Level IV AA Students will:
EE3.MID.H. 3 Compare data on a completed picture graph or bar graph to tell how many more and how many less.
Level III AA Students will:
EE3.MD.H. 3 Use a completed picture graph or bar graph to determine which has more and which has less (e.g., colors, weather, candy, shoes, height).

## Level II AA Students will:

EE3.MD.H. 3 Use a picture graph or bar graph to sort a given data set (e.g., colors, weather, candy, shoes, height).

## Level I AA Students will:

EE3.MD.H. 3 Use a picture graph or bar graph to sort 2 given data sets (e.g., colors, weather, candy, shoes, height).

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

3.MD.H. 4 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Use the data to create a line plot, where the horizontal scale is marked off in appropriate units-whole numbers, halves, or quarters.

## Geometric measurement:

understand concepts of area and relate area to multiplication and addition. (I)
3.MD.I. 5 Understand area as an attribute of plane figures and understand concepts of area measurement, such as square units without gaps or overlaps.
3.MD.I. 6 Measure areas by counting unit squares (square cm, square $m$, square in, square ft, and improvised units).
3.MD.I. 7 Relate area to the operations of multiplication and addition.
A. Find the area of a rectangle with whole-number side lengths (dimensions) by multiplying them. Show that this area is the same as when counting unit squares.
B. Multiply side lengths to find areas of rectangles with wholenumber side lengths in the context of solving real-world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.
C. Use area models to represen the distributive property in mathematical reasoning. Use tiling to show in a concrete case that the area of a rectangle with

EE3.MD.H. 4 Use a ruler
to measure objects to the nearest inch.

EE3.MD.I. 5 Identify the length and width of a rectangle.

EE3.MD.I.6-7 Find the area of rectangles with whole number side lengths by counting unit squares of an area up to 30.

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| whole-number side lengths a <br> and $b+c$ is the sum of $a \times b$ <br> and $a \times c$. |  |  |
| :--- | :--- | :--- |
| Geometric measurement: <br> recognize perimeter as an <br> attribute of plane figures and <br> distinguish between linear and <br> area measures. (J) <br> 3.MD.J.8 Solve real-world and <br> mathematical problems involving <br> perimeters of polygons, including finding <br> the perimeter given the side lengths, <br> finding an unknown side length, and <br> exhibiting rectangles with the same <br> perimeter and different areas or with the <br> same area and different perimeters. | EE3.MD.J.8 Not <br> applicable. | ***The Extended Standards Educator Committee determined there are no real-world <br> applications for this standard that are appropriate for this population and/or they <br> have been covered in previous standards. |
| 2018 Wyoming Mathematics <br> Content Standards | 2020 Wyoming Math |  |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content Standards

Operations and Algebraic Thinking
Use the four operations with whole numbers to solve problems. (A)
4.OA.A. 1 Intentionally removed in general ed. standard.
4.OA.A. 2 Multiply or divide to solve word problems involving multiplicative comparison, by using strategies including, but not limited to, drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison.
4.OA.A. 3 Solve multi-step word problems posed with whole numbers, including problems in which remainders must be interpreted.
A. Represent these problems using equations with a letter standing for the unknown quantity.
B. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.
Gain familiarity with factors and multiples. (B)
4.OA.B. 4 Demonstrate an understanding of factors and multiples.
A. Find all factor pairs for a whole number in the range 1-100.
B. Recognize that a whole number is a multiple of each of its factors.
C. Determine whether a given whole number in the range $1-100$ is a multiple of a given one-digit number.
D. Determine whether a given whole number in the range $1-100$ is prime or composite.

2020 Wyoming Math
Extended Standards

## Grade 4

## EE4.OA.A. 1

Intentionally removed.

EE4.OA.A.2-3 Solve given multiplication and division problems using appropriate strategies.
*This standard is intentionally repeated from 3.OA.A.3.

## Instructional Achievement Level Descriptor (ALDS)

** Standard 4.OA.2-3 were combined due to the similar nature of solving word problems.
Level IV AA Students wiil:
EE4.0A.A.2-3 Match a given multiplication or division equation with an appropriate one-step word problem.
Level III AA Students will:
EE4.0A.A.2-3 Solve given multiplication and division problems using appropriate strategies.
Level II AA Students will:
EE4.0A.A.2-3 Solve given multiplication or division problems using appropriate modeling strategies.
Level AA Students will:
EE4.0A.A.2-3 Identify an equation as a multiplication or division problem.

Level IV AA Students will:
EE.4.OA.B. 4 Identify the first ten multiples of 1, 2, 5, and 10.
Level III AA Students will:
EE.4.OA.B. 4 Identify the first five multiples of 1, 2, 5, and 10.

## Level II AA Students will:

EE.4.OA.B. 4 Identify the first five multiples of 1 and 10, as well as 2 or 5 .
Level I AA Students will:
EE.4.OA.B. 4 Identify the first five multiples of 1 and 10.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| Generate and analyze patterns. (C) <br> 4.OA.C. 5 Given a pattern, explain the rule that the pattern follows and extend the pattern. Generate a number or shape pattern that follows a given rule. Identify apparent features of the pattern that were not explicit in the rule itself. | EE4.OA.C. 5 Identify arithmetic patterns in addition and multiplication. <br> *This benchmark is intentionally a repeat of EE3.OA.D.9. | Level IV AA Students will: <br> EE4.OA.C. 5 Expand arithmetic patterns in addition and multiplication. Level III AA Students will: <br> EE4.OA.C. 5 Identify arithmetic patterns in addition and multiplication. Level II AA Students will: <br> EE4.OA.C. 5 Expand an arithmetic pattern in addition or multiplication. Level I AA Students will: <br> EE4.OA.C. 5 Identify an arithmetic pattern in addition or multiplication. |
| :---: | :---: | :---: |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Number and Operations Base Ten | Grade 4 |  |
| Generalize place value understanding for multi-digit whole numbers. (D) (limited to numbers less than or equal to $1,000,000$ ) <br> 4.NBT.D. 1 Recognize that in a multidigit whole number, a digit in one place represents ten times what it represents in the place to its right. | Recognize the value of <br> places. [Extended expectations in this <br> whole numbers up to but not including 1,000 ]. | Level IV AA Students will: <br> EE4.NBT.D. 1 Recognize the value of the number in the tens place is greater than the number in the ones place. <br> Level III AA Students vill: <br> EE4.NBT.D 1 Recognize the value of the number in the ones, tens, and hundreds places. <br> Level II AA Students will: <br> EE4.NBT.D. 1 Recognize the value of the number in the ones, tens, or hundreds places. <br> Level I AA Students will: <br> EE4.NBT.D. 1 Identify the digits in the ones, tens, and hundreds places. |
| 4.NBT.D. 2 Read and write multi-digit whole numbers using base-ten numerals, number names, and expanded form. Compare two multidigit numbers based on meanings of the digits in each place, using $>,=$, and < symbols. | Compare 2 multi-digit <br> [Extended expectations <br> numbers up to but not | Level IV AA Students will: <br> EE4.NBT.D. 2 Use symbols to compare 2 multi-digit numbers within one thousand (<, >, =). <br> Level III AA Students will: <br> EE4.NBT.D. 2 Compare 2 multi-digit numbers within one thousand. <br> Level II AA Students will: <br> EE4.NBT.D. 2 Compare 2 multi-digit numbers within one hundred. <br> Level I AA Students will: <br> EE4.NBT.D. 2 Compare 2 two-digit numbers within fifty. |
| 4.NBT.D. 3 Use place value understanding to round multi-digit whole numbers to any place. | EE4.NBT.D. 3 Round two-digit numbers from $10-100$, to the nearest 10. <br> [Extended expectations in this domain are limited to whole | Level IV AA Students will: <br> EE4.NBT.D. 3 Round three-digit numbers to the nearest 100. <br> Level III AA Students will: <br> EE4.NBT.D. 3 Round two-digit numbers from 10-100, to the nearest 10. <br> Level II AA Students will: <br> EE4.NBT.D. 3 Round two-digit numbers from 10-50, to the nearest 10. Level I AA Students will: |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Use place value understanding and properties of operations to perform multi-digit arithmetic. (E) (limited to whole numbers less than or equal to $1,000,000$ ). 4.NBT.E. 4 Add and subtract multidigit whole numbers using place value strategies including the standard algorithm.
4.NBT.E. 5 Use strategies based on place value and the properties of multiplication to:
A. Multiply a whole number of up to four digits by a one-digit whole number.
B. Multiply a pair of two-digit numbers.
C. Use appropriate models to explain the calculation, such as by using equations, rectangular arrays, and/or area models.
4.NBT.E. 6 Use strategies based on place value, the properties of multiplication, and/or the relationship between multiplication and division to find quotients and remainders with up to four-digit dividends and one-digit divisors. Use appropriate models to explain the calculation, such as by using equations, rectangular arrays, and/or area models.
numbers up to but not
including 1,000].
EE4.NBT.E. 4 Add or
subtract within 1000 using strategies or algorithms.

EE4.NBT.E. 5 Multiply one digit by two digit numbers by using arrays, equations, or models.

EE4.NBT.E. 6 Given a number up to 30, determine if a number is divisible by 5 and 10 , using strategies, arrays or area models.

EE4.NBT.D. 3 When given numbers 1-9, determine if the given number is rounded down to 0 or up to 10 .
Level IV AA Students will:
EE4.NBT.E. 4 Add and subtract within 1000 using strategies or algorithms.
Level III AA Students will:
EE4.NBT.E. 4 Add or subtract within 1000 using strategies or algorithms.
Level II AA Students will:
EE4.NBT.E. 4 Add and subtract within 100 using strategies or algorithms.

## Level I AA Students will:

EE4.NBT.E. 4 Add or subtract within 100 using strategies or algorithms.
Level IV AA Students will:
EE4.NBT.E. 5 Multiply one digit by three digit numbers.
Level III AA Students will:
EE4.NBT.E. 5 Multiply one digit by two digit numbers by using arrays, equations, or models.
Level II AA Students will:
EE4.NBT.E. 5 Build and use an array to demonstrate a one digit by one digit multiplication problem.
Level I AA Students will:
EE4.NBT.E. 5 Use a multiplication table to multiply one digit numbers with one digit numbers.

## Level IV AA Students will:

EF4.NBT.E. 6 Given a number up to 50 , determine if a number is divisible by 2,5 , and 10.
Level III AA Students will:
EE4.NBT.E. 6 Given a number up to 30, determine if a number is divisible by 5 and 10 , using strategies, arrays or area models.
Level II AA Students will:
EE4.NBT.E. 6 Use repeated addition to solve a given division problem with dividends to 20.
Level I AA Students will:
EE4.NBT.E. 6 When given multiples of 10 break it into equal groups of 5 or 10.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

## Number and Operations - Fractions

Extend understanding of fraction equivalence and ordering. (F) (limited to denominators $2,3,4,5,6,8,10,12$, and 100)
4.NF.F. 1 Explain why a fraction $a / b$ is equivalent to a fraction $(n \times a) /(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. Use this principle to recognize and generate equivalent fractions.
4.NF.F. 2 Compare two fractions with different numerators and different denominators by creating common denominators or numerators, or by comparing to a benchmark fraction such as $1 / 2$.
A. Recognize that comparisons are valid only when the two fractions refer to the same whole.
B. Record the results of comparisons with symbols >, $=$, or $<$.
C. Justify the conclusions by using a visual fraction model.

Build fractions from unit fractions by applying and extending previous understandings of operations on whole numbers. (G)
4.NF.G. 3 Understand a fraction $a / b$ with $a>1$ as a sum of unit fractions (1/b).
A. Understand addition and subtraction of fractions as joining and separating parts referring to the same whole.
B. Decompose a fraction into a sum of fractions with the same denominator in more than one way, recording each decomposition by an equation. Justify decompositions by using a visual fraction model.
C. Add and subtract mixed numbers with like denominators by replacing each mixed number with an equivalent fraction, and/or by using properties of addition and the relationship between addition and subtraction.
D. Solve word problems involving addition and subtraction of fractions referring to the same whole and having like denominators.
4.NF.G. 4 Apply and extend an understanding of multiplication by multiplying a whole number and a fraction.
A. Understand a fraction $a / b$ as a multiple of $1 / b$.
B. Understand a multiple of $a / b$ as a multiple of $1 / b$, and use this understanding to multiply a fraction by a whole number.
C. Solve real-world problems involving multiplication of a fraction by a whole number, using visual fraction models and equations to represent the problem.

## 2020 Wyoming Math Instructional Achievement Level Extended Standards

## Grade 4

EE4.NF.F.1-3 Use a visual fraction model to identify fractions with denominators of $2,3,4,5$, and 10. [Extended expectations in this domain are limited to fractions with denominators 2, 3, 4, 5 , 10].

EE4.NF.G. 4 Not applicable.

## Level IV AA Students will:

EE4.NF.F.1-3 Use a visual fraction model to compare equivalent fractions with
denominators of $2,3,4,5$ and 10.

## Leve! III AA Students will:

EE4.NF.F.1-3 Use a visual fraction model to identify fractions with denominators of $2,3,4,5$, and 10.
Level II AA Students will:
EE4.NF.F.1-3 Use a visual fraction model to compare one whole and one half.
Level I AA Students will:
EE4.NF.F.1-3 Use a visual fraction model to identify one whole and one half.

## ***The Extended Standards Educator

 Committee determined there are no realworld applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Understand decimal notation for fractions and compare decimal fractions. (H)
4.NF.H. 5 Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100
4.NF.H. 6 Use decimal notation for fractions with denominators 10 or 100. 4.NF.H. 7 Compare and order decimal numbers to hundredths and justify by using concrete and visual models. Record the results of comparisons with the words "is greater than," "is equal to," "is less than," and with the symbols >, =, and $<$.

EE4.NF.H. 5 Match a
fraction with a
denominator of ten with its equivalent model.

## EE4.NF.H.6-7 Identify

 the hundredths place.Level IV AA Students will:
EE4.NF.H. 5 Match a fraction with a denominator of one hundred with its equivalent model.
Level III AA Students will:
EE4.NF.H.5 Match a fraction with a denominator of ten with its equivalent model.
Level II AA Students will:
EE4.NF.H. 5 Using a fraction model, compare
fractions in units of ten.
Level I AA Students will:
EE4.NF.H. 5 Using a fraction model, identify
fractions in units of ten.
Level IV AA Students will:
EE4.NF.H.6-7 Identify a fraction with a
denominator of ten as a decimal.
Level III AA Students will:
EE4.NF.H.6-7 Identify the hundredths place.
Level II AA Students will:
EE4.NF.H.6-7 Identify the tenths place.
Level I AA Students will:
EE4.NF.H.6-7 Identify a decimal.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

## Measurement and Data

Solve problems involving measurement and conversion of measurements from a larger unit to a smaller unit. (I)
4.MD.I. 1 Know relative sizes of measurement units within one system of units including, but not limited to, $\mathrm{km}, \mathrm{m}, \mathrm{cm} ; \mathrm{kg}, \mathrm{g}$; $\mathrm{lb}, \mathrm{oz}$.; $\mathrm{L}, \mathrm{ml}$; hr, min, sec; ft, in, gal, qt, pt, c. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. Record measurement equivalents in a two-column table.
4.MD.I. 2 Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving simple fractions or decimals, and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale. Assessment Boundary: Use denominators of 2, 4, 8 and decimals up to hundredths.
4.MD.I. 3 Apply the area and perimeter formulas for rectangles in real-world and mathematical problems.

2020 Wyoming Math
Extended Standards

## Grade 4

EE4.MD.I.1-2 Measure objects using standard units within one system of units including, but not limited to, $k m, m, c m ; k g$, g; lb, oz.; L, ml; hr, min, sec; ft, in, gal, qt, pt, c.

## Level IV AA Students will

EE4.MD.I.1-2 Solve simple addition or subtraction problems using the same standard units of measurement including, but not limited to, $k m, m, c m ; k g, g ; l b, o z . ; ~ L, ~ m / ;$ hr, min, sec; ft, in, gal, qt, pt, c.
Level III AA Students will:
EE4.MD.I.1-2 Measure objects using standard units within one system of units including, but not limited to, $\mathrm{km}, \mathrm{m}, \mathrm{cm}$; kg, g; lb, oz.; L, ml; hr, min, sec; ft, in, gal, qt, pt, c.
Level II AA Students will:
EE4.MD.I.1-2 Identify standard units of measure using objects within one system of units including, but not limited to, $\mathrm{km}, \mathrm{m}, \mathrm{cm} ; \mathrm{kg}, \mathrm{g}$; lb, oz.; L, ml; hr, min, sec; ft, in, gal, qt, $p t, c$.
Level I AA Students will:
EE4.MD.I.1-2 Select the appropriate tool to measure a solid or a liquid.
Level IV AA Students will:
EE4.MD.I. 3 Find the perimeter of a rectangle within the range of 4-50.
Level III AA Students will:
EE4.MD.I. 3 Find the perimeter of a rectangle within the range of 4-20.
Level II AA Students will:
EE4.MD.I. 3 Identify a strategy to find the perimeter of a rectangle.

## Level I AA Students will

EE4.MD.I. 3 Identify the perimeter of a rectangle.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| Represent and interpret data. (J) <br> 4.MD.J. 4 Make a line plot to display a data set of measurements in fractions of a unit ( $1 / 2,1 / 4,1 / 8$ ). Solve problems involving addition and subtraction of fractions by using information presented in line plots. | EE4.MD.J. 4 <br> Given a line plot with whole numbers, place given half numbers to complete the line plot. | Level IV AA Students will: <br> EE4.MD.J. 4 Make a line plot to display a data set of whole and half numbers. <br> Level III AA Students will: <br> EE4.MD.J. 4 Given a line plot with whole numbers, place given half numbers to complete the line plot. <br> Level II AA Students will: <br> EE4.MD.J. 4 Identify whole and half numbers on a line plot. <br> Level I AA Students will: <br> EE4.MD.J. 4 Identify a line plot. |
| :---: | :---: | :---: |
| Geometric measurement: understand concepts of angle and measure angles. (K) <br> 4.MD.K. 5 Regarding angles: <br> A. Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint. <br> B. Understand concepts of angle measurement. An angle is measured with reference to a circle with its center at the common endpoint of the rays. | EE4.MD.K. 5 Identify an angle. | Level IV AA Students will: <br> EE4.MD.K. 5 Identify angles within a geometric shape. <br> Level III AA Students will: <br> EE4.MD.K. 5 Identify an angle. <br> Level II AA Students will: <br> EE4.MD.K. 5 Identify that two rays with a common endpoint form an angle. <br> Level I AA Students will: <br> EE4.MD.K. 5 Identify a ray. |
| 4.MD.K. 6 Measure angles in wholenumber degrees using a protractor. Sketch angles of specified measure. | EE4.MD.K. 6 Identify the measurement of a labeled angle. | Level IV AA Students will: <br> EE 4.MD.K. 6 Measure or sketch angles of various sizes. <br> Level III AA Students will: <br> EE4.MD.K. 6 Identify the measurement of a labeled angle. <br> Level II AA Students will: <br> EE4.MD.K. 6 Identify that angles can be different sizes. <br> Level I AA Students will: <br> EE4.MD.K. 6 Identify an angle. |
| 4.MD.K. 7 Solve addition and subtraction problems to find unknown angles on a diagram in real-world and mathematical problems. | EE4.MD.K. 7 Not applicable. | ***The Extended Standards Educator Committee determined there are no realworld applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |

Wyoming Department of Education edu.wyoming.gov/standards

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards <br> 2020 Wyoming Math <br> Extended Standards

## Geometry

Draw and identify lines and angles and classify shapes by properties of their lines and angles. (L)
4.G.L. 1 Draw points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. Identify these in twodimensional figures.
4.G.L. 2 Classify two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. Recognize right triangles as a category, and identify right triangles.
4.G.L. 3 Identify line-symmetric figures. Recognize and draw lines of symmetry for two-dimensional figures.

## Instructional Achievement Level Descriptor (ALDs)

## Grade 4

EE4.G.L.1-2 Identify points, lines, angles.

Level IV AA Students will:
EE4.G.L.1-2 Draw one of the following: points, lines or
angles. Level III AA Students will:

## EE4.G.L.1-2 Identify points, lines, angles

Level II AA Students will:
EE4.G.L.1-2 Identify two of the following points, lines or angles.
Level I AA Students will:
EE4.G.L1-2 Identify one of the following: points, lines or angles.
***The Extended Standards Educator Committee determined there are no realworld applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

## Operations and Algebraic Thinking

Write, interpret, and/or evaluate numerical expressions. (A)
5.OA.A. 1 Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.
5.OA.A. 2 Write simple expressions requiring parentheses that record calculations with numbers, and interpret numerical expressions without evaluating them.

Analyze patterns and relationships. (B)
5.OA.B. 3 Generate two numerical patterns with each pattern having its own rule. Explain informally the relationship(s) between corresponding terms in the two patterns.
A. Form ordered pairs consisting of corresponding terms from the two patterns.
B. Graph the ordered pairs on a coordinate plane.

Numbers and Operations in Base Ten
Understand the place value system.

## (C)

5.NBT.C. 1 Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $1 / 10$ of what it represents in the place to its left.

## 2020 Wyoming Math

Extended Standards

## Grade 5

EE5.OA.A.1-2 Identify the first step in solving a two-step number sentence using parentheses.

## Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EE5.OA.A.1-2 Solve the first step in a two-step number sentence with parentheses.
Level III AA Students will:
EE5.OA.A.1-2 Identify the first step in solving a two-step number sentence using parentheses.
Level II AA Students will:
EE5.OA.A.1-2 Identify parentheses in a number sentence.
Level I AA Students will:
EE5.OA.A.1-2 Solve single digit addition and subtraction problems within a sum or difference of 10 to 20.
Level IV AA Students will:
EE5.OA.B.3.a-b When given a one-step rule, extend the whole number pattern.
Level III AA Students will:
EE5.OA.B.3.a-b Match a rule to its appropriate whole number pattern.
Level II AA Students will:
EE5.OA.B.3.a-b Identify the given rule of a one-step whole number pattern. Level I AA Students will:
EE5.OA.B.3.a-b Identify a whole number pattern.

## Level IV AA Students will:

EE5.NBT.C. 1 Identify the value of the digit in the tenths place.
Level III AA Students will:
EE5.NBT.C. 1 Identify the tenths, hundredths, and thousandths place value. Level II AA Students will:
EE5.NBT.C. 1 Identify the tenths and hundredths place value.
Level I AA Students will:
EE5.NBT.C. 1 Identify the tenths or hundredths place value.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

5.NBT.C. 2 Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10. Use whole-number exponents to denote powers of 10 .
5.NBT.C. 3 Read, write, and compare decimals to thousandths.
A. Read and write decimals to thousandths using base-ten numerals, number names, and expanded form.
B. Compare two decimals to thousandths based on meanings of the digits in each place, using $>,=$, and < symbols.
5.NBT.C. 4 Use place value understanding to round decimals to any place to a given place.
Assessment Boundary: Given place value to the thousandths.
Perform operations with multi-digit whole numbers and with decimals to hundredths. (D)
5.NBT.D. 5 Multiply multi-digit whole numbers using place value strategies including the standard algorithm.
5.NBT.D.6 Find whole-number quotients with up to four-digit dividends and two-digit divisors, using strategies based on place value, the properties of multiplication, and/or the relationship between multiplication and division, including the standard algorithm. Use appropriate models to Illustrate and explain the calculation, such as equations, rectangular arrays, and/or area models. Assessment Boundary: The standard algorithm for division will not be assessed.

EE 5.NBT.C. 2 Order multiples of thousands ranging from 1000 9000, from least to greatest.

EE 5.NBT.C.3-4 Read and write decimals to the tenths place.

EE5.NBT.D.5-6 Multiply and divide three digit by one digit numbers with no remainders.

Level IV AA Students will:
EE5.NBT.C. 2 Using multiples of tens, hundreds, or thousands extend a pattern within the range of 10 to 9000 .

## Level III AA Students will:

EE 5.NBT.C. 2 Order multiples of thousands ranging from 1000-9000, from least to greatest.
Level II AA Students will:
EE 5.NBT.C. 2 Order multiples of hundreds ranging from 100-900, from least to greatest.
Level I AA Students will:
EE 5.NBT.C. 2 Order multiples of ten ranging from 10-90, from least to greatest.
Level IV AA Students will:
EE 5.NBT.C.3-4 Compare two decimal models to the tenths place using $>$, $=$, and < symbols.
Level III AA Students will:
EE 5.NBTC.3-4 Read and write decimals to the tenths place.
Level II AA Students will:
EE 5.NBT.C.3-4 Read or write a decimal to the tenths place.
Level AA Students will:
EE 5.NBT.C.3-4 Identify a decimal.

## Level IV AA Students will:

EE5.NBT.D.5-6 Multiply and divide four digit by one digit numbers with no remainders.

## Level III AA Students will:

EE5.NBT.D.5-6 Multiply and divide three digit by one digit numbers with no remainders.
Level II AA Students will:
EE5.NBT.D.5-6 Multiply and divide two digit by one digit numbers with no remainders.
Level I AA Students will:
EE5.NBT.D.5-6 Multiply and divided one digit by one digit numbers with no remainders.

Wyoming Department of Education
edu.wyoming.gov/standards

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

5.NBT.D. 7 Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used.

## 2018 Wyoming Mathematics

Content Standards

## Number and Operations - Fractions

Use equivalent fractions as a strategy to add and subtract fractions. (E)
5.NF.E. 1 Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators.
5.NF.E. 2 Solve word problems involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem. Use benchmark fractions and number sense of fractions to estimate mentally and assess the reasonableness of answers.

EE5.NBT.D. 7 Add decimals in the tenths place.

## 2020 Wyoming Math

Extended Standards

## Grade 5

## 5.NF.E.1-2 Add

fractions with like denominators (halves, thirds, fourths).

Level IV AA Students will:
EE5.NBT.D. 7 Add and subtract decimals in the tenths place.
Level III AA Students will:
EE5.NBT.D. 7 Add decimals in the tenths place.
Level II AA Students will:
EE5.NBT.D. 7 Match decimal models of addition and subtraction to their sum or difference.
Level I AA Students will:
EE5.NBT.D. 7 Identify decimals to the tenths place.
Instructional Achievement Level Descriptor (ALDs)

Level IV AA Students will:
EE5.NF.E.1-2 Add and subtract fractions with like denominators (halves, thirds, fourths).
Level III AA Students will:
EE5.NF.E.1-2 Add fractions with like denominators (halves, thirds, fourths).
Level II AA Students will:
EE5.NF.E.1-2 Identify halves, thirds, and fourths.

## Level AA Students will:

EE5.NF.E.1-2 Match halves, thirds, and fourths.
**Word problems are not applicable to this group of students

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Apply and extend previous understandings of multiplication and division to multiply and divide fractions. (F)
5.NF.F. 3 Interpret a fraction as division of the numerator by the denominator ( $a / b=a \div b$ ). Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers by using visual fraction models or equations to represent the problem.
5.NF.F. 4 Extend the concept of multiplication to multiply a fraction or whole number by a fraction.
A. Recognize the relationship between multiplying fractions and finding the areas of rectangles with fractional side lengths.
B. Interpret multiplication of a fraction by a whole number and a whole number by a fraction and compute the product.
C. Interpret multiplication in which both factors are fractions less than one and compute the product.
5.NF.F. 5 Justify the reasonableness of a product when multiplying with fractions.
A. Estimate the size of the product based on the size of the two factors.
B. Explain why multiplying a given number by a number greater than 1 (improper fractions, mixed numbers, whole numbers) results in a product larger than the given number.
C. Explain why multiplying a given number by a fraction less than 1 results in a product smaller than the given number.
D. Explain why multiplying the numerator and denominator by the same number has the same effect as multiplying the fraction by 1.
5.NF.F. 6 Solve real-world problems involving multiplication of fractions and mixed numbers by using visual fraction models or equations to represent the problem.
5.NF.F. 7 Extend the concept of division to divide unit fractions and whole numbers by using visual fraction models and equations.
A. Interpret division of a unit fraction by a non-zero whole number and compute the quotient.
B. Interpret division of a whole number by a unit fraction and compute the quotient.
C. Solve real-world problems involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions by using visual fraction models and equations to represent the problem.

EE5.NF.F.3-7 Not applicable.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| :---: | :---: | :---: |
| Measurement and Data | Grade 5 |  |
| Convert like measurement units within a given measurement system. (G) 5.MD.G. 1 Solve multi-step real-world problems by converting among different-sized standard measurement units within a given measurement system. | like units of but not limited to, km, ml; hr, min, sec; ft, in, | Level IV AA Students will: <br> EE5.MD.G. 1 Order like units of measurement from greatest to least including but not limited to, km, m, cm; kg, $g ; \mathrm{lb}, o z \cdot L, m l ; h r$, min, sec; ft, in, gal, qt, pt, c. <br> Level III AA Students will: <br> EE5.MD.G. 1 Categorize like units of measurement including but not limited to, $\mathrm{km}, \mathrm{m}, \mathrm{cm} ; \mathrm{kg}, \mathrm{g} ; \mathrm{lb}$, oz.; L, m/; hr, min, sec; ft, in, gal, qt, pt, c. <br> Level II AA Students will: <br> EE5.MD.G. 1 Match 5 units with appropriate measurement tools. <br> Level I AA Students will: <br> EE5.MD.G. 1 Identify 5 units of measurement. |
| Represent and interpret data. (H) 5.MD.H. 2 Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, 1/8). Use operations on fractions to solve problems involving information presented in line plots. | EE5.MD.H. 2 Place given wholes, halves, and fourths on a line plot. | Level IV AA Students will: <br> EE5.MD.H. 2 Make a line plot to display a data set of wholes, halves, and fourths. <br> Level III AA Students will: <br> EE5.MD.H. 2 Place given wholes, halves, and fourths on a line plot. <br> Level Il AA Students will: <br> EE5.MD.H. 2 Identify wholes, halves, and fourths on a line plot. <br> Level I AA Students will: <br> EE5.MD.H. 2 Identify wholes and halves on a line plot. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Geometric measurement: understand concepts of volume and relate volume to multiplication and addition. (I)
5.MD.I. 3 Recognize volume as an attribute of three-dimensional figures and understand concepts of volume measurement such as "unit cube" and a volume of $n$ cubic units.
5.MD.I. 4 Measure volumes by counting unit cubes, using cubic cm, cubic in, cubic ft, and improvised units.
5.MD.I. 5 Relate volume to the operations of multiplication and solve real-world and mathematical problems involving volume.
A. Find the volume of a right rectangular prism with whole number dimensions by multiplying them. Show that this volume is the same as when counting unit cubes.
B. Find volumes of right rectangular prisms with whole-number edge lengths in the context of solving realworld and mathematical problems given the formulas $V=(I)(w)(h)$ and $V$ $=(B)(h)$ for rectangular prisms.

## 2018 Wyoming Mathematics

Content Standards

## Geometry

Graph points on the coordinate plane to solve real-world and mathematical problems. (J)
5.G.J. 1 Understand a coordinate system.
A. The $x$ - and $y$-axes are perpendicular number lines that intersect at 0 (the origin)
B. Any point on the coordinate plane can be represented by its coordinates.
C. The first number in an ordered pair is the $x$-coordinate and represents the horizontal distance from the origin.
D. The second number in an ordered pair is the $y$-coordinate and

## EE5.MD.I.3-5

Determine the volume of a rectangular prism by counting unit cubes up to a total volume of 30.

Level IV AA Students will:
EE5.MD.I.3-5 Determine that volume can be measured in different units: including but not limited to cubic cm, cubic in, cubic ft.

## Level III AA Students will:

EE5.MD.I.3-5 Determine the volume of a rectangular prism by counting unit cubes up to a total volume of 30 .
Level II AA Students will:
EE5.MD.I.3-5 Identify three-dimensional figures have volume.
Level I AA Students will:
EE5.MD.I.3-5 Identify three-dimensional figures.

Instructional Achievement Level Descriptor (ALDs)
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

represents the vertical distance from the origin.
5.G.J. 2 Plot and interpret points in the first quadrant of the coordinate plane to represent real-world and mathematical situations.
Classify two-dimensional figures into categories based on their properties. (K)
5.G.K. 3 Understand that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category Assessment Boundary: Use polygons only. 5.G.K. 4 Classify polygons in a hierarchy based on properties.

EE5.G.K.3-4 Sort attributes of quadrilaterals and triangles.

Level IV AA Students will: EE5.G.K.3-4 Compare attributes of quadrilaterals and triangles.
Level III AA Students will:
EE5.G.K.3-4 Sort attributes of quadrilaterals and triangles.
Level II AA Students will:
EE5.G.K.3-4 Identify attributes of quadrilaterals and triangles.
Level I AA Students will:
EE5.G.K.3-4 Identify quadrilaterals and triangles.
** Standards 5.G.3 and 5.G.4 require complementary skills; therefore, they were combined.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics

 Content Standards
## Ratios and Proportional

## Relationships

Understand ratio concepts and use ratio reasoning to solve problems. (A)
6.RP.A. 1 Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities.
6.RP.A. 2 Understand the concept of a unit rate $a / b$ associated with a ratio $a: b$ with $b \neq 0$, and use rate language in the context of a ratio relationship.
6.RP.A. 3 Use ratio and rate reasoning to solve real-world and mathematical problems.
A. Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.
B. Solve unit rate problems including those involving unit pricing and constant speed.
C. Understand that a percentage is a rate per 100 and use this to solve problems involving

2020 Wyoming Math
Extended Standards

## Grade 6

EE6.RP.A. 1 Describe relationships between two quantities.

EE6.RP.A. 2 Understand a unit rate can be expressed in two forms. a/b associated with a ratio $a: b$ with $b \neq 0$.

EE6.RP.A. 3 Understand that a percentage is a rate per 100 involving wholes, parts, and percentages.

## Instructional Achievement Level Descriptor (ALDS)

## Level IV AA Students will:

EE6.RP.A. 1 Use ratio language to describe a relationship using numbers or objects.
Level III AA Students will:
EE6.RP.A. 1 Describe ratio relationships between two quantities.
Level II AA Students will:
EE6.RP.A. 1 Match items according to a simple ratio relationship.
Level I AA Students will:
EE6.RP.A. 1 Identify a one-to-one relationship. (Indicate each object using touch, hand over hand, eye gaze, etc.).
Level IV AA Students will:
EE6.RP.A. 2 Determine the unit rate between two quantities.
Level III AA Students will:
EE6.RP.A. 2 Understand a unit rate can be expressed in two forms. a/b associated with a ratio $a: b$ with $b \neq 0$.
Level II AA Students will:
EE6.RP.A. 2 Match equal unit rates in the form of $a / b$ or $a: b$ using numerical values. Level IAA Students will:
EE6.RP.A. 2 When given a unit rate, use objects to represent the ratio.
Level IV AA Students will:
EE6.RP.A. 3 Understand that a percentage is a rate per 100 and apply to solve real world problems involving wholes, parts, and percentages.

## Level III AA Students will:

EE6.RP.A. 3 Understand that a percentage is a rate per 100 involving wholes, parts, and percentages.
Level II AA Students will:
EE6.RP.A. 3 Recognize a percent from a rate per 100.
Level I AA Students will:
EE6.RP.A. 3 Select the percent sign from a variety of math symbols/signs.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| wholes, parts, and percentages. <br> D. Use ratio reasoning to convert measurement units; convert units appropriately when multiplying or dividing quantities. |  |  |
| :---: | :---: | :---: |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| The Number System | Grade 6 |  |
| Apply and extend previous understandings of multiplication and division to divide fractions by fractions. (B) <br> 6.NS.B. 1 Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions by using visual fraction models and equations to represent the problem. | EE6.NS.B. 1 Use a fraction model to compute the quotient of a natural number, up to 20, divided by a fraction. Limit divisors to $1 / 4,1 / 3$, $1 / 2$. | Level IV AA Students will: <br> EE6.NS.B. 1 Solve a word problem using a fraction model to compute the quotient of a natural number, up to 20 , divided by a fraction. Limit divisors to $1 / 4,1 / 3,1 / 2$. <br> Level III AA Students will: <br> EE6.NS.B. 1 Use a fraction model to compute the quotient of a natural number, up to 20 , divided by a fraction. Limit divisors to $1 / 4,1 / 3,1 / 2$. <br> Level II AA Students will: <br> EE6.NS.B. 1 Use a fraction model to divide a natural number, up to 10, into halves and quarters with no remainders. <br> Level I AA Students will: <br> EE6.NS.B. 1 Match a fraction to the corresponding model of the fraction. |
| Compute fluently with multi-digit numbers and find common factors and multiples. (C) <br> 6.NS.C. 2 Divide multi-digit numbers using efficient and generalizable procedures including, but not limited to the standard algorithm. <br> Assessment Boundary: Use up to 5digit dividend, 2-digit divisors. | EE6.NS.C. 2 Divide a two-digit number by a one-digit number without remainders. | Level IV AA Students will: <br> EE6.NS.C. 2 Divide a three-digit number by a one- or two-digit number without remainders. <br> Level III AA Students will: <br> EE6.NS.C. 2 Divide a two-digit number (between 21 and 99) by a one-digit <br> number without remainders. <br> Level II AA Students will: <br> EE6.NS.C. 2 Divide a two-digit number, up to 20, by a one-digit number without remainders. <br> Level I AA Students will: <br> EE6.NS.C. 2 Divide a one-digit number by a one-digit number without remainders. |
| 6.NS.C. 3 Add, subtract, multiply, and divide manageable multi-digit decimals using efficient and generalizable procedures including, but not limited to the standard algorithm for each operation. | EE6.NS.C. 3 Add and subtract two multi-digit numbers with decimals up to the hundredths place. | Level IV AA Students will: <br> EE6.NS.C. 3 Multiply two multi-digit numbers with decimals up to the tenths place. <br> Level III AA Students will: <br> EE6.NS.C. 3 Add and subtract two multi-digit numbers with decimals up to the hundredths place. <br> Level II AA Students will: <br> EE6.NS.C. 3 Add and subtract two multi-digit numbers up to the tenths place without regrouping. |

Wyoming Department of Education edu.wyoming.gov/standards

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| :---: | :---: |
| 6.NS.C. 4 Find common factors and multiples using two whole numbers. <br> A. Find the greatest common factor of two whole numbers less than or equal to 100. <br> B. Find the least common multiple of two whole numbers less than or equal to 12 . <br> C. Use the distributive property to express a sum of two whole numbers $1-100$ with a common factor as a multiple of a sum of two whole numbers with no common factor. | EE6.NS.C. 4 Find common factors and multiples using two whole numbers. <br> A.) Find the greatest common factor of two whole numbers less than or equal to 100 with factors of 2,5 , and/or 10. <br> B.) Find the least common multiple of two whole numbers each of which is less than or equal to 10. |
| Apply and extend previous understandings of numbers to the system of rational numbers. <br> (D) <br> 6.NS.D. 5 Understand that positive and negative numbers are used together to describe quantities having opposite directions or values and use them to represent quantities in realworld contexts, explaining the meaning of 0 in each situation. | EE6.NS.D. 5 Using a model, locate positive and negative numbers and their opposite values. |
| 6.NS.D. 6 Extend the understanding of the number line to include all rational numbers and apply this concept to the coordinate plane. <br> A. Understand the concept of opposite numbers, including zero, and their relative locations on the number line. <br> B. Understand that signs of numbers in ordered pairs indicate locations in quadrants of the coordinate plane, recognize that when two ordered pairs differ only by | EE6.NS.D. 6 When given a coordinate plane with a scale of 1 , understand that signs of numbers in ordered pairs represent locations in quadrants. |

## Level I AA Students will:

EE6.NS.C. 3 Add two multi-digit numbers up to the tenths place without regrouping.

## Level IV AA Students will:

EE6.NS.C. 4 Use the distributive property to express a sum of two whole numbers 1-50 with a common factor as a multiple of a sum of two whole numbers with no common factor.

## Level III AA Students will:

EE6.NS.C. 4 Find common factors and multiples using two whole numbers.
A. Find the greatest common factor of two whole numbers less than or equal to 100 with factors of 2,5 , and 10 .
B. Find the least common multiple of two whole numbers each of which is less than or equal to 10 .
Level II AA Students will:
EE6.NS.C. 4 List the factors of two whole numbers less than or equal to 50 with factors of 2, 5, and 10 .
Level I AA Students will:
EE6.NS.C. 4 Identify muiliples of 2, 5, and 10.

## Level IV AA Students will:

EE6.NS.D. 5 Apply positive and negative numbers in real-world contexts.
Level til AA Students will:
EE6.NS.D. 5 Using a model, locate positive and negative numbers and their opposite values.
Level II AA Students will:
EE6.NS.D. 5 Using a model, locate positive and negative numbers and their opposite values.
Level I AA Students will:
EE6.NS.D. 5 Using a model, locate positive numbers.

## Level IV AA Students will:

EE6.NS.D. 6 When given an ordered pair with integers, find the position on a coordinate plane with a scale of 1.

## Level III AA Students will:

EE6.NS.D. 6 When given a coordinate plane with a scale of 1, understand that signs of numbers in ordered pairs represent locations in quadrants.

## Level II AA Students will:

EE6.NS.D. 6 When given an ordered pair ( $a, b$ ), $a$ and $b>0$, understand the value of the numbers in the ordered pair represent positions $(a, 0)$ on the horizontal axis and $(0, b)$ and the vertical axis.
Level I AA Students will:
EE6.NS.D. 6 Label the horizontal axis, vertical axis, and quadrants on a coordinate plane.

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| signs, the locations of the points are related by reflections across one or both axes. <br> C. Find and position rational numbers on a horizontal or vertical number line diagram; find and position pairs of rational numbers on a coordinate plane. |  |  |
| :---: | :---: | :---: |
| 6.NS.D. 7 Understand ordering and absolute value of rational numbers. <br> A. Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram. <br> B. Write, interpret, and explain statements of order for rational numbers in real-world contexts. <br> C. Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a realworld situation. <br> D. Distinguish comparisons of absolute value from statements about order. | EE6.NS.D. 7 Understand ordering of rational numbers using a model. | Level IV AA Students will: <br> EE6.NS.D. 7 Interpret statements of inequality using rational numbers in real-world contexts. <br> Level III AA Students will: <br> EE6.NS.D. 7 Understand ordering of rational numbers using a model. <br> Level II AA Students will: <br> EE6.NS.D. 7 Understand ordering of positive rational numbers using a model. <br> Level I AA Students will: <br> EE6.NS.D. 7 Understand ordering of whole numbers using a model. |
| 6.NS.D. 8 Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Find distances between points with the same first coordinate or the same second coordinate; relate absolute value and distance. | EE6.NS.D. 8 Find the vertical and horizontal distance from $(0,0)$ to given points in the coordinate plane. | Level IV AA Students will: <br> EE6.NS.D. 8 Find the vertical and horizontal distance from $(0,0)$ to given points in the coordinate plane in a real-world context. <br> Level III AA Students will: <br> EE6.NS.D. 8 Find the vertical and horizontal distance from $(0,0)$ to given points in the coordinate plane. <br> Level II AA Students will: <br> EE6.NS.D. 8 Find the vertical or horizontal distance from $(0,0)$ to a given point in the coordinate plane. <br> Level I AA Students will: |

# DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS 

|  |  | EE6.NS.D. 8 Identify ( 0,0 ) in a coordinate plane. |
| :---: | :---: | :---: |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (A) |
| Expressions and Equations | Grade 6 |  |
| Apply and extend previous understandings of arithmetic to algebraic expressions. (E) 6.EE.E. 1 Write and evaluate numerical expressions involving wholenumber exponents. | EE6.EE.E. 1 Write a numerical expression using $2,3,4$, and 5 as exponents. | Level IV AA Students will: <br> EE6.EE.E. 1 Evaluate a numerical expression using 2 and 3 as exponents. <br> Level III AA Students will: <br> EE6.EE.E. 1 Write a numerical expression using 2, 3, 4, and 5 as exponents. <br> Level II AA Students will: <br> EE6.EE.E. 1 Match an exponential expression to its expanded form. <br> Level I AA Students will: <br> EE6.EE.E. 1 Identify the exponent in an exponential expression. |
| 6.EE.E. 2 Write, read, and evaluate expressions in which letters stand for numbers. <br> A. Write expressions that record operations with numbers and with letters standing for numbers. <br> B. Identify parts of an expression using mathematical terms (sum, difference, term, product, factor, quotient, coefficient, constant). <br> C. Use Order of Operations to evaluate algebraic expressions at using positive rational numbers and whole-number exponents. Include expressions that arise from formulas in real-world problems. | EE6.EE.E.2a Evaluate an expression in which a letter stands for a number. <br> EE6.EE.E.2b Use Order of Operations to list the sequence of operations needed to evaluate algebraic expressions with whole numbers. | Level IV AA Students will: <br> EE6.EE.E.2a Write and evaluate an expression in which a letter stands for a number. <br> EE6.EE.E.2b Use Order of Operations to list the sequence of operations needed to evaluate algebraic expressions with whole numbers and whole number exponents. <br> Level III AA Students will: <br> EE6.EE.E.2a Evaluate an expression in which a letter stands for a number. <br> EE6.EE.E.2b Use Order of Operations to list the sequence of operations needed to evaluate algebraic expressions with whole numbers. <br> Level II AA Students will: <br> EE6.EE.E.2a Given an expression with an unknown, produce a model which represents the expression. <br> EE6.EE.E.2b Use Order of Operations, not including exponents and parentheses, to list the sequence of operations needed to evaluate algebraic expressions with whole numbers. <br> Level I AA Students will: <br> EE6.EE.E.2a Use a picture to give meaning to a letter that represents a number. <br> EE6.EE.E.2b Use Order of Operations, not including exponents and parentheses, to list the sequence of operations needed to evaluate algebraic expressions with whole numbers. |
| 6.EE.E. 3 Apply the properties of operations to generate equivalent expressions. <br> 6.EE.E. 4 Identify when two expressions are equivalent. | EE6.EE.E.3-4 When comparing two equivalent expressions, select which one property of operations is used. | Level IV AA Students will: <br> EE6.EE.E.3-4 Formulate an expression that represents one of the properties of operations. <br> Level III AA Students will: <br> EE6.EE.E.3-4 When comparing two equivalent expressions, select which one property of operations is used. <br> Level II AA Students will: |


|  |  | EE6.EE.E.3-4 When comparing two equivalent expressions, determine whether the distributive or commutative property is used. <br> Level I AA Students will: <br> EE6.EE.E.3-4 Match equivalent expressions using the commutative property. |
| :---: | :---: | :---: |
| Reason about and solve onevariable equations and inequalities. (F) <br> 6.EE.F. 5 Understand a solution to an equation or an inequality makes the equation or inequality true. Use substitution to determine whether a given number in a specified set makes an equation or inequality true. | EE6.EE.F. 5 Use substitution to determine whether a given natural number in a specified set is a solution to an equation. | Level IV AA Students will: <br> EE6.EE.F. 5 Use substitution to determine whether a given natural number in a specified set makes an equation or inequality true. <br> Level III AA Students will: <br> EE6.EE.F. 5 Use substitution to determine whether a given natural number in a specified set is a solution to an equation. <br> Level II AA Students will: <br> EE6.EE.F. 5 Use substitution to determine whether a given natural number in the set $\{1,2, \ldots 10\}$ is a solution to an equation. <br> Level I AA Students will: <br> EE6.EE.F. 5 Determine whether a given list of statements is true or false. <br> e.g., $2=2$ is true, $2=3$ is false; e.g., 1 elephant $=1$ elephant is true |
| 6.EE.F. 6 Use variables to represent unknown numbers and write expressions when solving a real-world or mathematical problem. | EE6.EE.F. 6 When given a real-world problem, use a variable to represent an unknown number. | Level IV AA Students will: <br> EE6.EE.F. 6 Use a variable to write an expression that represents a real-world problem <br> Level til AA Students will: <br> EE6.EE.F. 6 When given a real-world problem, use a variable to represent an unknown number. <br> Level II AA Students will: <br> EE6.EE.F. 6 Match models to a set of variables. <br> Level I AA Students will: <br> EE6.EE.F. 6 Match a model to a specified variable. |
| 6.EE.F. 7 Write and solve real-world and mathematical problems in the form of one-step, linear equations involving non-negative rational numbers. | EE6.EE.F. 7 Recognize a one-step linear equation in a realworld context. | Level IV AA Students will: <br> EE6.EE.F. 7 Solve a one-step linear equation in a real-world context. <br> Level III AA Students will: <br> EE6.EE.F. 7 Recognize a one-step linear equation in a real-world context. <br> Level II AA Students will: <br> EE6.EE.F. 7 Recognize a one-step linear equation involving natural numbers. <br> Level I AA Students will: <br> EE6.EE.F. 7 Identify a linear pattern. |
| 6.EE.F. 8 Write an inequality of the form $x>c$ or $x<c$ to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form $x>c$ or $x<$ $c$ have infinitely many solutions; | EE6.EE.F. 8 Choose the one-step inequality that is modeled by a number line. | Level IV AA Students will: <br> EE6.EE.F. 8 Illustrate the one-step inequality that is modeled by a number line. <br> Level III AA Students will: <br> EE6.EE.F. 8 Choose the one-step inequality that is modeled by a number line. <br> Level II AA Students will: <br> EE6.EE.F. 8 Identify one solution to a one-step inequality. |

represent solutions of such inequalities on number line diagrams.

## Represent and analyze

 quantitative relationships between dependent and independent variables. (G)6.EE.G. 9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity (dependent variable), in terms of the other quantity (independent variable). Analyze their relationship using graphs and tables, and relate these to the equation.

## 2018 Wyoming Mathematics

 Content Standards
## Geometry

## Solve real-world and

 mathematical problems involving area, surface area, and volume. (H)6.G.H.1 Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems.
6.G.H. 2 Find the volume of a right rectangular prism with fractional edge lengths in the context of solving realworld and mathematical problems by applying the formulas $V=(I)(w)(h)$ and $V=(B)(h)$, and label with appropriate units.

EE6.EE.G. 9 Use a table of values to plot at least three integer ordered pairs on a coordinate plane.

## 2020 Wyoming Math

 Extended Standards
## Grade 6

EE6.G.H. 1 Given
formulas and a labeled diagram with height, find the area of triangles and quadrilaterals.

## EE6.G.H. 2 Given a

 labeled diagram, find the volume of a right rectangular prism with natural number side lengths by applying the formula $V=(I)(w)(h)$.Level I AA Students will:
EE6.EE.F. 8 Select inequalities from a given list that includes one-step equations.
Level IV AA Students will:
EE6.EE.G. 9 Given a graph, complete a table of values.
Level III AA Students will:
EE6.EE.G.9 Use a table of values to plot at least three integer ordered pairs on a coordinate plane.
Level II AA Students will:
EE6.EE.G. 9 Match a table of values to a graph.
Level I AA Students will:
EE6.EE.G.9 Identify one ordered pair from a graph.

## Instructional Achievement Level Descriptor (ALDs)

## Level IV AA Students will:

EE6.G.H. 1 Given formulas, find the area of triangles and quadrilaterals in a realworld context.
Level III AA Students will:
EE6.G.H. 1 Given formulas and a labeled diagram with height, find the area of triangles and quadrilaterals.
Level II AA Students will:
EE6.G.H. 1 Given formulas and a labeled diagram with height, find the area of a square and rectangle.
Level I AA Students will:
EE6.G.H. 1 Given a formula and a labeled diagram, find the area of a square.
Level IV AA Students will:
EE6.G.H. 2 Given a labeled diagram, find the volume of a right rectangular prism with natural numbers by applying the formula $V=(I)(w)(h)$, and label with appropriate units.

## Level III AA Students will:

EE6.G.H. 2 Given a labeled diagram, find the volume of a right rectangular prism with natural number side lengths by applying the formula $V=(I)(w)(h)$.

## Level II AA Students will:

EE6.G.H. 2 Given a labeled diagram, find the volume of a cube with natural numbers by applying the formula $V=(I)(w)(h)$.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

|  |  | Level I AA Students will: <br> EE6.G.H.2 Given a diagram of a cube and rectangular prism, label the length, width, <br> and height. |
| :--- | :--- | :--- |
| 6.G.H.3 Draw polygons in the <br> coordinate plane given coordinates for <br> the vertices; use coordinates to find <br> the length of a side joining points with <br> the same first coordinate or the same <br> second coordinate. Apply these <br> techniques in the context of solving <br> real-world and mathematical problems. | EE6.G.H.3 Connect the <br> coordinates of a <br> rectangle and determine <br> each side length. | Level IV AA Students will: <br> EE6.G.H.3 Draw quadrilaterals in the coordinate piane given coordinates for the <br> vertices, and find the length of each side. <br> Level III AA Students will: |
| EE6.G.H.3 Connect the coordinates of a rectangle and determine each side length. |  |  |
| Level II AA Students will: |  |  |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

6.SP.I. 2 Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape.
6.SP.I. 3 Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number.

## Summarize and describe

 distributions. (J)6.SP.J. 4 Display numerical data in plots on a number line, including dot plots, stem-and-leaf plots, histograms, and box plots.

EE6.SP.I.2-3 Recognize
data can be
summarized using a single number to answer a statistical question.

EE6.SP.J. 4 Recognize
a visual example of a number line, dot plot (line plot), and histogram.

Level IV AA Students will:
EE6.SP.I.2-3 Discuss the center, spread, and/or shape of the data as it relates to a statistical question.

## Level III AA Students will:

EE6.SP.I.2-3 Recognize data can be summarized using a single number to answer a statistical question.
Level II AA Students will:
EE6.SP.I.2-3 Create a summarizing statement about the data provided.
Level I AA Students will:
EE6.SP.I.2-3 Select a statement that summarizes the data provided.
Level IV AA Students will:
EE6.SP.J. 4 Display data using one of the following charts: number line, dot plot
(line plot), or histogram.
Level III AA Students will:
EE6.SP.J. 4 Recognize a visual example of a number line, dot plot (line plot), and histogram.
Level II AA Students will:
EE6.SP.J.4 Recognize a visual example of two of the following three representations: a number line, dot plot (line plot), or histogram.
Level 1 AA Students will:
EE6.SP.J. 4 Recognize a visual example of one of the following three
representations: a number line, dot plot (line plot), or histogram.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

6.SP.J.5 Summarize numerical data sets in relation to their real-world context.
A. Report the sample size.
B. Describe the context of the data under investigation, including how it was measured and its units of measurement.
C. Find quantitative measures of center (median, mode and mean) and variability (range and interquartile range). Describe any overall pattern (including outliers, clusters, and distribution), with reference to the context in which the data was gathered.
D. Justify the choice of measures of center (median, mode, or mean) based on the shape of the data distribution and the context in which the data was gathered.

EE6.SP.J. 5 Find data attributes which include outliers, clusters, sample size, mean, median, mode, and range from a visual representation of the data.

Level IV AA Students will:
EE6.SP.J.5 Find and discuss data attributes which include outliers, clusters,
sample size, mean, median, mode, and range from a visual representation of the data in a real-world context.
Level III AA Students will:
EE6.SP.J. 5 Find data attributes which include outliers, clusters, sample size, mean, median, mode, and range from a visual representation of the data.
Level II AA Students will:
EE6.SP.J. 5 Identify any outliers, clusters, and the sample size from a visual representation.
Level I AA Students will:
EE6.SP.J. 5 Identify any outliers and clusters from a visual representation.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| :---: | :---: | :---: |
| Ratios and Proportional Relationships | Grade 7 |  |
| Analyze proportional relationships and use them to solve real-world and mathematical problems. (A) <br> 7.RP.A. 1 Compute unit rates, including those involving complex fractions, with like or different units. | EE7.RP.A. 1 Compute whole number unit rates with natural numbers. | Level IV AA Students will: <br> EE7.RP.A. 1 Compute unit rates with natural numbers. <br> Level III AA Students will: <br> EE7.RP.A. 1 Compute whole number unit rates with natural numbers. <br> Level II AA Students will: <br> EE7.RP.A. 1 Recognize the components of a unit rate problem. <br> Level I AA Students will: <br> EE7.RP.A. 1 Select a unit rate from a list of rates. |
| 7.RP.A. 2 Recognize and represent proportional relationships between quantities. <br> A. Decide whether two quantities in a table or graph are in a proportional relationship. <br> B. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships. <br> C. Represent proportional relationships with equations. <br> D. Explain what a point $(x, y)$ on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0,0)$ and $(1, r)$ where $r$ is the unit rate. | EE7.RP.A. 2 Discuss a proportional relationship for a given representation. | Level IV AA Students will: <br> EE7.RP.A. 2 Decide whether two quantities in a table or graph are in a proportional relationship. <br> Level III AA Students will: <br> EE7.RP.A. 2 Discuss a proportional relationship for given multiple representations. <br> Level II AA Students will: <br> EE7.RP.A. 2 Select a proportional relationship for a given representation. <br> Level I AA Students will: <br> EET.RP.A. 2 Define a proportional relationship. |
| 7.RP.A. 3 Solve multi-step real-world and mathematical problems involving ratios and percentages. | EE7.RP.A. 3 Solve a real-world two-step problem involving percentages. | Level IV AA Students will: <br> EE7.RP.A. 3 Solve a real-world two-step problem involving ratios and percentages. <br> Level III AA Students will: <br> EE7.RP.A. 3 Solve a real-world two-step problem involving percentages. <br> Level II AA Students will: <br> EE7.RP.A. 3 Solve a two-step problem involving percentages. <br> Level I AA Students will: <br> EE7.RP.A. 3 Given a list of numbers identify the numbers with the percent symbol. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

2020 Wyoming Math Extended Standards

Instructional Achievement Level Descripior (ALDs)

## Grade 7

EE7.NS.B. 1 Understand that a number and its opposite sum to zero and a number plus zero does not change the value of the original number.

## EE7.NS. B.2a

Understand that a number and its reciprocal multiply to one and that a number multiplied by one does not change the value of the original number.

## EE7.NS.B.2b

Understand positive and negative sign rules for multiplying and dividing

Level IV AA Students will:
EE7.NS.B. 1 Use a model to illustrate that a number and its opposite sum to zero and a number plus zero does not change the value of the original number in a real-world context.
Level III AA Students will:
EE7.NS.B. 1 Understand that a number and its opposite sum to zero and a number plus zero does not change the value of the original number.
Level II AA Students will:
EE7.NS.B. 1 When given a list of integer values, identify their opposites. Level I AA Students will:
EE7.NS.B. 1 Identify opposite values of integers using a visual representation.

## Level IV AA Students will:

EE7.NS.B.2a Develop equations to illustrate that a number and its reciprocal multiply to one, or that a number times one does not change the value of the original number.
EE7.NS.B.2b Understand positive and negative sign rules for multiplying and dividing integers where zero is not the divisor. Interpret products of integers by describing real-world contexts.
EE7.NS.B.2c Simplify expressions using properties of multiplication to multiply rational numbers.
EE7.NS.B.2d Convert a rational number to a decimal. Recognize that the decimal is terminating or repeating.
Level III AA Students will:

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

B. Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers is a rational number. Recognize that if $p$ and $q$ are integers then $-(p / q)=(-p) / q=p /(-q)$. Interpret quotients of rational numbers by describing real-world contexts.
C. Apply properties of multiplication (commutative, associative, distributive, or properties of identity and inverse elements) to multiply and divide rational numbers.
D. Convert a rational number to a decimal. Recognize that rational numbers can be written as fractions or decimal numbers that terminate or repeat.
7.NS.B. 3 Solve real-world and mathematical problems involving the four arithmetic operations with rational numbers. (Computations with rational numbers extend the rules for manipulating fractions to complex fractions.)
integers where zero is not the divisor.

EE7.NS.B.2c Simplify expressions using properties of multiplication of integers

EE7.NS.B.2d Convert a rational number to a decimal.

EE7.NS.B. 3 Solve two step real-world mathematical probiems involving the four arithmetic operations with rational numbers.

EE7.NS.B.2a Understand that a number and its reciprocal multiply to one and that a number multiplied by one does not change the value of the original number.
EE7.NS.B.2b Understand positive and negative sign rules for multiplying and dividing integers where zero is not the divisor.
EE7.NS.B.2c Simplify expressions using properties of multiplication of integers.

## EE7.NS.B.2d Convert a rational number to a decimal.

## Level II AA Students will:

EE7.NS.B.2a Identify the reciprocal values of integers.
EE7.NS.B.2b Understand positive and negative sign rules for multiplying or dividing integers where zero is not the divisor.
EE7.NS.B.2c Simplify expressions.
EE7.NS.B.2d Convert a rational number to a decimal, such as $1 / 4,1 / 2$,
1/10.
Level AA Students will:
EET.NS.B.2a Identify the reciprocal values of positive integers.
EE7.NS.B.2b Multiplying integers.
EE7.NS.B.2c Identify expressions.
EE7.NS.B.2d Match a decimal to its fractional equivalent.

## Level IV AA Students will:

EE7.NS.B. 3 Solve multiple-step real-world mathematical problems involving the four arithmetic operations with rational numbers.

## Level III AA Students will:

EE7.NS.B. 3 Solve two-step real-world mathematical problems involving the four arithmetic operations with rational numbers.

## Level II AA Students will:

EE7.NS.B. 3 Solve one-step real-world mathematical problems involving the four arithmetic operations with rational numbers.

## Level I AA Students will:

EE7.NS.B. 3 Solve one-step real-world mathematical problems involving the four arithmetic operations with integers.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics

 Content Standards
## Expressions and Equations

Use properties of operations to generate equivalent expressions.

## (C)

7.EE.C. 1 Apply properties of operations as strategies to add, subtract, factor, and expand linear expressions with rational coefficients.
7.EE.C. 2 Recognize that algebraic expressions may have a variety of equivalent forms that reveal different information, and determine an appropriate form for a given real-world situation.
Solve real-life and mathematical problems using numerical and algebraic expressions and equations. (D)
7.EE.D. 3 Solve multi-step real-world and mathematical problems involving rational numbers. Include fraction bars as a grouping symbol.
7.EE.D. 4 Apply the concepts of linear equations and inequalities in one variable to real-world and mathematical situations.
A. Write and fluently solve linear equations of the form $a x+b=c$ and $a(x+b)=c$ where $a, b$, and $c$ are rational numbers.
B. Write and solve multi-step linear equations that include the use of the distributive property-and combining like terms. Exclude equations that contain variables on both sides.

2020 Wyoming Math
Extended Standards

## Grade 7

EE7.EE.C.1-2 Use the relationship within addition and/or multiplication to illustrate that two expressions are equivalent.

EE7.EE.D. 3 Solve twostep real-world and mathematical addition and subtraction equations using rational numbers.

EE7.EE.D. 4 Solve onestep linear equations with one variable.

## Instructional Achievement Level Descriptor (AL.Ds)

## Level IV AA Students will:

EE7.EE.C.1-2 Use the relationship within addition and/or multiplication to illustrate that two expressions are equivalent for a given real-world situation. Level III AA Students will:
EE7.EE.C.1-2 Use the relationship within addition and/or multiplication to illustrate that two expressions are equivalent.

## Level II AA Students will:

EE7.EE.C.1-2 Match two equivalent expressions.
Level I AA Students vill:
EE7.EE.C.1-2 Identify if two expressions are equivalent.

## Level IV AA Students will:

EE7.EE.D. 3 Solve two-step real-world and mathematical equations using rational numbers.
Level III AA Students will:
EE7.EE.D. 3 Solve two-step real-world and mathematical addition and subtraction equations using rational numbers.
Leve II AA Students will:
EE7.EE.D. 3 Solve two-step real-world and mathematical equations using integers.
Level I AA Students will:
EE7.EE.D. 3 Solve one-step real-world and mathematical equations using integers.
Level IV AA Students will:
EE7.EE.D. 4 Solve one-step linear equations with one variable and graph.
Level III AA Students will:
EE7.EE.D. 4 Solve one-step linear equations with one variable.
Level II AA Students will:
EE7.EE.D. 4 Identify the solution to a one-step linear equation with one variable on a graph.
Level I AA Students will:
EE7.EE.D. 4 Identify a linear graph.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| C. Write and solve two-step linear <br> inequalities. Graph the solution <br> set on a number line and interpret <br> its meaning. |  |  |
| :--- | :--- | :--- |
| D. <br> Identify and justify the steps for <br> solving multi-step linear equations <br> and two-step linear inequalities. |  |  |
| 2018 Wyoming Mathematics <br> Content Standards | 2020 Wyoming Math <br> Extended Standards | Instructional Achievement Level Descriptor (AL.Ds) |

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|  |  |
| :--- | :--- |
| Solve real-life and mathematical <br> problems involving angle measure, <br> area, surface area, and volume. (F) <br> 7.G.F.4 Investigate the concept of <br> circles. <br> A. Demonstrate an understanding of <br> the proportional relationships <br> between diameter, radius, and <br> circumference of a circle. | p |
| and |  |
| B.Understand that pi is defined by <br> the constant of proportionality <br> betwent the circumference and <br> diameter. |  |
| C. Given the formulas for |  |
| circumference and area of circles, |  |
| solve real-world and |  |
| mathematical problems. |  |

## Solve real-life and mathematical

 problems involving angle measure, area, surface area, and volume. (F) 7.G.F. 4 Investigate the concept of ircles.Demonstrate an understanding of the proportional relationships circumference of a circle.
B. Understand that pi is defined by eonstant of proportionality between the circumference and
C. Given the formulas for circumference and area of circles, solve real-world and mathematical problems.
7.G.F. 5 Use facts about supplementary, complementary, vertical, and adjacent angles in a multi-step problem to write and solve simple equations for an unknown angle in a figure.
7.G.F. 6 Solve real-world and A. Area problems involving objects composed of triangles and quadrilaterals;
only of right prisms triangular or quadrilaterar bases.

EE7.G.F.4.A-C Given the
formulas for the area and circumference of a circle use them to solve problems.

## EE7.G.F. 5 Find the

 missing angle given a relationship (adjacent, supplementary, and complementary) of two angles and one of their measures.
## EE7.G.F. 6 Solve

 mathematical problems invoiving area, volume and surface area of twoand three-dimensional objects composed of triangles, rectangles, cubes, rectangular prisms and triangular
## Level I AA Students will:

EE7.G.E.3 Replicate the two-dimensional cross-section of a three-dimensional shape (cube, pyramid, rectangular prism) when given a complete shape.

## Level IV AA Students will:

EE7.G.F.4.A-C Given the formulas for the area and circumference of a circle, use them to solve problems for real-world problems.

## Level III AA Students will:

EE7.G.F.4.A-C Given the formulas for the area and circumference of a circle, use them to solve problems.
Level II AA Students will:
EE7.G.F.4.A-C Identify the parts of a circle within the formulas for area and circumference.

## Level I AA Students vill:

EE7.G.F.4.A-C Identify the parts of a circle (diameter, radius, and circumference).

## Level IV AA Students will:

EE7.G.F. 5 Find the missing angle given a relationship (adjacent, supplementary, vertical, and complementary) of two angles and one of their measures.
Level III AA Students will:
EE7.G.F. 5 Find the missing angle given a relationship (adjacent, supplementary, and complementary) of two angles and one of their measures.
Level II AA Students will:
EE7.G.F. 5 Find the missing angle given a relationship (supplementary and complementary) of two angles and one of their measures.

## Level I AA Students will:

EE7.G.F. 5 Find the missing angle given a relationship (complementary) of two angles and one of their measures.

## Level IV AA Students will:

EE7.G.F. 6 Solve real-world mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, rectangles, cubes, rectangular prisms and triangular prisms when given the formulas.

## Level III AA Students will:

EE7.G.F. 6 Solve mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, rectangles, cubes, rectangular prisms and triangular prisms when given the formulas. Level II AA Students will:

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

|  | prisms when given the <br> formulas. | EE7.G.F.6 Solve mathematical problems involving area and volume of two- <br> and three-dimensional objects composed of triangles, rectangles, cubes, <br> rectangular prisms and triangular prisms when given the formulas. <br> Level I AA Students will: |
| :--- | :--- | :--- |
| EE7.G.F.6 Recognize the difference between volume and area. |  |  |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

data (e.g., back-to-back stem and leaf plots, dot plots, histograms, box plots) that are graphed on the same scale and draw inferences about this data.
7 SP H 4 Given measures of center and
7.SP.H. 4 Given measures of center and variability (mean, median and/or mode; range, interquartile range, and/or standard deviation), for numerical data from random samples, draw appropriate informal comparative inferences about two populations.

Investigate chance processes and develop, use, and evaluate probability models. (I)
7.SP.I. 5 Find and interpret the probability of a random event. Understand that the probability of a random event is a number between, and including 0 and 1 that expresses the likelihood of the event occurring
graph) and make two inferences based on the comparison.

EE7.SP.H. 4 Given
variability (mean,
median and/or mode; and range), for
populations.

EE7.SP.I. 5 Understand that the probability of a random event occurring expresses the likelihood of the event.

EE7.SP.H. 3 Compare two sets of data within a single data display such as a picture graph, line plot, or bar graph, and make two inferences based on the comparison.

## Level II AA Students will:

EE7.SP.H. 3 Summarize data on a graph or table in one way.

## Level I AA Students will:

EE7.SP.H. 3 Read data from one given source.
Level IV AA Students will:
EE7.SP.H.4 Given measures of center and variability (mean, median and/or mode; range), for numerical questions make inferences about populations in real-world situations.

## Level III AA Students will

EE7.SP.H. 4 Given measures of center and variability (mean, median and/or mode; and range), for numerical data make inferences about populations.

## Level II AA Students will:

EE7.SP.H. 4 Given measures of center and variability (mean, and range), for numerical data make inferences about populations.

## Level I AA Students will:

EE7.SP.H 4 Given measures of center and variability (mean and range), for numerical data answer questions about populations.

## Level IV AA Students will:

EE7.SP.I. 5 Understand that the probability of a random event occurring
expresses the likelihood of the event in a real-world situation.

## Level III AA Students will:

EE7.SP.I.5 Understand that the probability of a random event occurring expresses the likelihood of the event.

## Level II AA Students will:

EE7.SP.I. 5 Given a set of data understand that the probability of an event occurring expresses the likelihood of the event.

## Level I AA Students will:

EE7.SP.I. 5 Identify a probability.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

7.SP.I. 6 Collect multiple samples to compare the relationship between theoretical and experimental probabilities for simple events.
7.SP.I.7 Apply the concepts of theoretical and experimental probabilities for simple events.
A. Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events.
B. Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.
C. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancies.
7.SP.I. 8 Find probabilities of compound events using organized lists, tables, and tree diagrams.
A. Understand that, just as with simple events, the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs.
B. Represent sample spaces for compound events using methods such as organized lists, tables, and tree diagrams. For an event described in everyday language (e.g., "rolling double sixes"), identify the outcomes in the sample space which compose the event.

EE7.SP.I. 6 When given a question, do an experiment multiple times; then compare the outcomes to the expected results of an event occurring.

EE7.SP.I.7-8 Not applicable.

Level IV AA Students will:
EE7.SP.I.6 Create a question; then do an experiment multiple times; then compare the outcomes to the expected results of an event occurring.

## Level III AA Students will:

EE7.SP.I. 6 When given a question, do an experiment multiple times; then compare the outcomes to the expected results of an event occurring.

## Level II AA Students will:

EE7.SP.I. 6 Given data about an experiment done multiple times compare the outcomes to the expected results of an event occurring.
Level I AA Students will
EE7.SP.I. 6 Match the probability to an outcome of an event.
***The Extended Standards Educator Committee determined there are no real-worid applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content Standards

The Number System
Know that there are numbers that are not rational, and approximate them by rational numbers. (A)
8.NS.A. 1 Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number. Explore the real number system and its appropriate usage in real-world situations.
A. Make comparisons between rational and irrational numbers.
B. Understand that all real numbers have a decimal expansion.
C. Model the hierarchy of the real number system, including natural, whole,
integer, rational, and irrational numbers.
D. Convert repeating decimals to fractions.
8.NS.A. 2 Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions.

2020 Wyoming Math
Extended Standards

## Grade 8

EE8.NS.A. 1 Identify
both terminating and repeating decimal patterns as rational.

## Instructional Achievement Level Descriptor (ALDs)

## Level IV AA Students will:

EE8.NS.A. 1 Identify decimals that neither terminate nor repeat as irrational, such as Pi or sq. root ( ${ }^{2}$ ).

## Level III AA Students will:

EE8.NS.A. 1 Identify both terminating and repeating decimal patterns as rational.

## Level II AA Students will:

EE8.NS.A. 1 Identify a terminating decimal as rational.

## Level I AA Students will.

EE8.NS.A. 1 Convert simple fractions to decimal form, such as $1 / 2,1 / 4,1 / 5,1 / 8$, 1/10

Level IV AA Students will:
EE8.NS.A. 2 Approximately locate irrational representations on a number line, such as Pi or sq. root ( ${ }^{2}$ ).
Level III AA Students will:
EE8.NS.A. 2 Locate fractional and decimal representations on a number line.
Level II AA Students will:
EE8.NS.A. 2 Plot a decimal that falls between two whole numbers (e.g., $0.75,1.5,4.25)$.
Level I AA Students will:
EE8.NS.A. 2 Locate whole numbers on a number line.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content |
| :--- | :--- | :--- |
| Standards |$\quad$| 2020 Wyoming Math |
| :--- |
| Extended Standards | Instructional Achievement Level Descriptor (ALDs)

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

8.EE.B. 3 Explore the relationship between quantities in decimal and scientific notation.
A. Express very large and very small quantities, $p$, in scientific notation in the form $a \times 10^{b}=p$ where 1 is less than or equal to $a$ and $a$ is less than 10 and $b$ is an integer.
B. Translate between decimal notation and scientific notation.
C. Estimate and compare the relative size of two quantities in scientific notation.
8.EE.B. 4 Apply the concepts of decimal and scientific notation to real-world and mathematical problems.
A. Select appropriate units of measure when representing answers in scientific notation.
B. Interpret scientific notation that has been generated by a variety of technologies.

Understand the connections between proportional relationships, lines, and linear equations. (C)
8.EE.C. 5 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways.
8.EE.C. 6 Explain why the slope $m$ is the same between any two distinct points on a nonvertical line in the coordinate plane; derive the equation $y=m x$ for a line through the origin and

EE8.EE.B. 3 Translate decimal notation and scientific notation. Limit values from millions to thousandths range using single digits.

EE8.EE.B. 4 Use mathematical problems to convert very large or very small quantities to scientific notation and simplify using metric conversions. Limit quantities from millions to thousandths.

EE8.EE.C. 5 When given data, create a graph and determine if the rate of change has a positive or negative relationship.

Level IV AA Students will:
EE8.EE.B. 3 Translate decimal notation and scientific notation.
Level III AA Students will:
EE8.EE.B. 3 Translate decimal notation and scientific notation. Limit values from millions to thousandths range using single digits.

## Level II AA Students will:

EE8.EE.B. 3 Given multiple numbers in scientific notation put them in ascending and/or descending order.

## Level I AA Students will:

EE8.EE.B. 3 Given scientific notation match this notation to its decimal equivalent.
Level IV AA Students will:
EE8.EE.B. 4 Use mathematical problems to convert very large or very small quantities to scientific notation and simplify using metric conversions.
Level III AA Students will:
EE8.EE.B. 4 Use mathematical problems to convert very large or very small quantities to scientific notation and simplify using metric conversions. Limit quantities from millions to thousandths.
Level II AA Students will:
EE8.EE.B. 4 Matching multiple equivalent expressions with scientific notation across different metric units.
Level I AA Students will:
EE8.EE.B. 4 Match a given metric decimal unit to its simplest form. (e.g., 1000 g to 1 kg )

## Level IV AA Students will:

EE8.EE.C. 5 Collect data, create a graph, and determine if the rate of change has a positive or negative relationship.
Level III AA Students will:
EE8.EE.C. 5 When given data, create a graph and determine if the rate of change has a positive or negative relationship.
Level II AA Students will:
EE8.EE.C. 5 When given multiple graphs determine which graphs have a rate of change that is positive/negative.

## Level I AA Students will:

EE8.EE.C. 5 Given a graph determine if the relationship is positive or negative.
Level IV AA Students will:
EE8.EE.C. 6 Given a simple integer based graph that goes through the origin, write the linear equation.
Level III AA Students will:
the equation $y=m x+b$ for a line intercepting the vertical axis at $(0, b)$.

Analyze and solve linear equations and pairs of simultaneous linear equations. (D)
8.EE.D. 7 Extend concepts of linear equations and inequalities in one variable to more complex multi-step equations and inequalities in realworld and mathematical situations.
A. Solve linear equations and inequalities with rational number coefficients that include the use of the distributive property, combining like terms, and variable terms on both sides.
B. Recognize the three types of solutions to linear equations: one solution, infinitely many solutions, or no solutions.
C. Generate linear equations with the three types of solutions.
D. Justify why linear equations have a specific type of solution.

## 8.EE.D. 8 Analyze and solve pairs of

 simultaneous linear equations.A. Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.
B. Solve systems of two linear equations in two variables with integer solutions by graphing the equations.
C. Solve simple real-world anc mathematical problems leading to two linear equations in two variables given $y$ $=m x+b$ form with integer solutions.
intercept in $y=m x+b$ form.

## EE8.EE.D. 7

Given an inequality, match it to the appropriate graph from a given selection of graphs, and determine if an ordered pair is a solution.

EE8.EE.C. 6 Write a linear equation given the slope and intercept in $\mathrm{y}=\mathrm{mx}$ +b form.

## Level II AA Students will:

EE8.EE.C. 6 Given a linear equation, identify siope and intercept .
Level I AA Students will:
EE8.EE.C. 6 Identify the slope.

## Level IV AA Students will:

EE8.EE.D. 7 Given an inequality, match it to the graph; then find an ordered pair that is a solution for the graph.
Level III AA Students will:
EE8.EE.D. 7 Given an inequality, match it to the appropriate graph from a given selection of graphs, and determine if an ordered pair is a solution. Level II AA Students wiII:
EE8.EE.D. 7 Given a coordinate and a graph, determine if it is a solution for a given inequality.

## Level I AA Students will:

EE8.EED. 7 Given an inequality graph and a linear graph, identify an inequality.

## Level IV AA Students will:

EE8.EE.D. 8 Given two equations, graph and solve the system.

## Level III AA Students will:

EE8.EE.D. 8 Given a graph of two linear equations, name the solution as an ordered pair.
Level II AA Students will:
EE8.EE.D. 8 Given an ordered pair, determine which graph represents the solution.

## Level I AA Students will:

EE8.EE.D. 8 Given a graph of two linear equations, identify their intersection.

DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content |
| :--- | :--- | :--- |
| Standards | | 2020 Wyoming Math |
| :--- |
| Extended Standards | Instructional Achievement Level Descriptor (ALDs)

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| D. Interpret the meaning of the slope and the $y$-intercept of a linear function in the context of the situation. |  |  |
| :---: | :---: | :---: |
| 8.F.F. 5 Describe qualitatively the functional relationship between two quantities by analyzing a graph where the function is increasing, decreasing, constant, linear, or nonlinear. Sketch a graph that exhibits the qualitative features of a function that has been described verbally. | EE8.F.F. 5 <br> When given a graph(s), determine if the function(s) is increasing or decreasing and/or linear or nonlinear. | Level IV AA Students will: <br> EE8.F.F. 5 When given a graph(s), explain how the function(s) is increasing or decreasing and/or linear or nonlinear. <br> Level III AA Students will: <br> EE8.F.F. 5 When given a graph(s), determine if the function(s) is increasing or decreasing and/or linear or nonlinear. <br> Level II AA Students will: <br> EE8.F.F. 5 When given linear graphs, determine if the functions are increasing or decreasing. <br> Level I AA Students will: <br> EE8.F.F. 5 When given two linear graphs, identify which is increasing/decreasing. |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Geometry | Grade 8 |  |
| Understand congruence and similarity using physical models, transparencies, or geometry software. (G) <br> 8.G.G. 1 Verify experimentally the properties of rotations, reflections, and translations. <br> A. Lines are taken to lines, and line segments to line segments of the same length. <br> B. Angles are taken to angles of the same measure. <br> C. Parallel lines are taken to parallel lines. | EE8.G.G. 1 Draw and transform a figure describing whether you used rotation, reflection, or translation. | Level IV AA Students will: <br> EE8.G.G. 1 Demonstrate understanding of rotation, reflection, and <br> translation by drawing the three on graph paper. <br> Level III AA Students will: <br> EE8.G.G. 1 Draw and transform a figure describing whether you used rotation, reflection, or translation. <br> Level II AA Students will: <br> EE8.G.G. 1 Draw and transform a figure using reflection or translation. <br> Level I AA Students will: <br> EE8.G.G. 1 When given a transformation, determine if it is a reflection or translation. |
| 8.G.G. 2 Recognize through visual comparison that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them. | EE8.G.G. 2 Use a transformation to align two objects to determine if they are congruent. | Level IV AA Students will: <br> EE8.G.G. 2 Use transformations to align objects to determine which objects are congruent to one another. <br> Level III AA Students will: <br> EE8.G.G. 2 Use a transformation to align two objects to determine if they are congruent. <br> Level II AA Students will: <br> EE8.G.G. 2 Use transformation to align two congruent objects. <br> Level I AA Students will: <br> EE8.G.G. 2 Determine if two objects are congruent. |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

8.G.G. 3 Describe the effect of dilations, translations, rotations, and reflections on twodimensional figures using coordinates.
8.G.G. 4 Recognize through visual comparison that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar twodimensional figures, describe a sequence that exhibits the similarity between them.
8.G.G.5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles.

Understand and apply the Pythagorean Theorem. (H)
8.G.H. 6 Use models or diagrams to explain the Pythagorean Theorem and its converse.

EE8.G.G. 3 When provided with a twodimensional figure and a dilation, provide an explanation of how the figure is dilated.

EE8.G.G. 4
Determine what sequence of two transformations were used to transform one figure to another.

EE8.G.G.5 When given a diagram of a triangle with the measurements for 2 angles within a triangle, find the measurement of the third angle.

EE8.G.H. 6 Label the hypotenuse and legs of a right triangle.

## Level IV AA Students will:

EE8.G.G. 3 Given coordinates, create a two-dimensional figure and demonstrate dilation.

## Level III AA Students will:

EE8.G.G. 3 When provided with a two-dimensional figure and a dilation, provide an explanation of how the figure is dilated.

## Level II AA Students will:

EE8.G.G. 3 Manipulate shapes to demonstrate dilation.
Level I AA Students will:
EE8.G.G. 3 When given a shape, identify whether a comparison shape is a dilation.
Level IV AA Students will
EE8.G.G. 4 Determine what sequence of multiple transformations, including a dilation, were used to transform one figure to another.
Level III AA Students will:
EE8.G.G. 4 Determine what sequence of two transformations were used to transform one figure to another.

## Level II AA Students will:

EE8.G.G. 4 Given two figures, match which two sequences formed the similar translated figure.

## Level I AA Students will:

EE8.G.G. 4 Identify if two figures are similar.
Level IV AA Students will:
EE8.G.G.5. Given a diagram of a triangle with an interior angle and two exterior angles, find the missing interior angles.
Level III AA Students will:
EE8.G.G.5 When given a diagram of a triangle with the measurements for 2 angles within a triangle, find the measurement of the third angle.
Level II AA Students will:
EE8.G.G. 5 Understand that all angles of a triangle add up to $180^{\circ}$.
Level I AA Students will:
EE8.G.G. 5 When shown a right triangle, determine which angle is a right angle and apply the right angle symbol.

## Level IV AA Students will:

EE8.G.H. 6 Using the variables and terms in the Pythagorean theorem label the legs and hypotenuse ( $\mathrm{a}, \mathrm{b}, \mathrm{c}$ ).
Level III AA Students will:
EE8.G.H. 6 Label the hypotenuse and legs of a right triangle.

## Level II AA Students will:

EE8.G.H. 6 Identify the longest leg of the right triangle

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

\(\left.$$
\begin{array}{|l|l|l|}\hline & & \begin{array}{l}\text { Level I AA Students will: } \\
\text { EE8.G.H.6 Identify a right triangle. }\end{array} \\
\hline \begin{array}{l}\text { 8.G.H.7 Apply the Pythagorean Theorem to } \\
\text { determine unknown side lengths in right } \\
\text { triangles in real-world and mathematical } \\
\text { problems. }\end{array} & \begin{array}{l}\text { EE8.G.H.7 Use the } \\
\text { Pythagorean theorem to } \\
\text { calculate the length of } \\
\text { the hypotenuse given } \\
\text { side a and side b. }\end{array} & \begin{array}{l}\text { Level IV AA Students will: } \\
\text { EE8.G.H.7 Use the Pythagorean theorem to calculate the length of a side } \\
\text { given a side and hypotenuse. } \\
\text { Level III AA Students will: } \\
\text { EE8.G. H.7 Use the Pythagorean theorem to calculate the length of the } \\
\text { hypotenuse given side a and side b. } \\
\text { Level II AA Students will: }\end{array}
$$ <br>
EE8.G.H.7 Put the values for sides a, b, and c into the correct locations <br>
for the Pythagorean theorem. <br>

Level I AA Students will:\end{array}\right]\)| EE8.G.H.7 Given the Pythagorean formula with numbers entered for the |
| :--- | :--- |
| values of a, b, and c, have the student determine which value is the |
| hypotenuse. |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics

 Content Standards2020 Wyoming Math
Extended Standards

## Instructional Achievement Level Descriptor (ALDs)

## Statistics and Probability

## Investigate patterns of association in

 bivariate data. (J)8.SP.J. 1 Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe the association by form (linear / nonlinear), direction (positive / negative), strength (correlation), and unusual features.
8.SP.J. 2 Know that straight lines are widely
used to model relationships between two
quantitative variables. For scatter plots that
suggest a linear association, informally fit a
straight line, and informally assess the model
fit by judging the closeness of the data points to the line.
8.SP.J. 3 Use an equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept.
8.SP.J. 4 Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table.
A. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects.

## Grade 8

EE8.SP.J. 1 Interpret scatter plots by describing the association between two quantities by form (linear/nonlinear) and direction (positive/negative).

## EE8.SP.J. 2 Use a

 straight lines within scatter plots to suggest a linear association by judging the closeness of the data points to the line.EE8.SP. 3.3 Not applicable.

EE8.SP.J. 4 Not applicable.

## Level IV AA Students will:

EE8.SP.J. 1 Interpret scatter plots by describing the association between two quantities by form (linear/nonlinear), direction (positive/negative), strength (correlation), and unusual features.

## Level III AA Students will:

EE8.SP.J. 1 Interpret scatter plots by describing the association between two quantities by form (linear/nonlinear) and direction (positive/negative).
Level II AA Students will:
EE8.SP.J. 1 When provided with a scatter plot, interpret the display by making at least one inference.

## Level I AA Students will:

EE8.SP.J. 1 When provided with a scatter plot, determine if the direction is positive/negative.
Level IV AA Students will:
EE8.SP. J. 2 Select a straight line of best fit within a scatter plot given multiple lines to suggest a linear association and describe the association.
Level III AA Students will:
EE8.SP.J. 2 Use a straight lines within scatter plots to suggest a linear association by judging the closeness of the data points to the line. Level II AA Students will:
EE8.SP.J. 2 Determine if a straight line could be placed on a scatter plot to show a linear association.

## Level I AA Students will:

EE8.SP.J. 2 Determine if a graph is a scatter plot.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

B. Use relative frequencies calculated for rows or columns to describe possible association between the two variables.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content

## Standards

NOTE: ( + ) designated for complex mathematics (advanced courses). These were not extended in the Extended Standards to the right of this document. A Table of the ( + ) standards can be found at the end of this document.

## Number and Quantity - The Real Number System

Extend the properties of exponents to rational exponents. (A)
N.RN.A. 1 Explain how the meaning of the definition of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents.
N.RN.A. 2 Rewrite expressions involving radicals and rational exponents using the properties of exponents.

## Use properties of rational and irrational

 numbers. (B)N.RN.B. 3 Explain why the sum or product of rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational.

2020 Wyoming Math Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## High School

EEN.RN.A. 1 Not applicable.

## EEN.RN.A. 2 Match the

 radical representation to its rational exponent form. Exponents limited to $1 / 2,1 / 3,1 / 4$.
## EEN.RN.B. 3 Not applicable.

***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Level IV AA Students will:
EEN.RN.A. 2 Given either the radical or rational exponent representation, write its equivalent representation. Level III AA Students will:
EEN.RN.A. 2 Match the radical representation to its rational exponent form. Exponents limited to $1 / 2,1 / 3,1 / 4$. (e.g., sq. root $\left.(x)=x^{\wedge}(1 / 2)\right)$ Level II AA Students will:
EEN.RN.A. 2 Identify the radical representation and/or rational exponential form.
Level I AA Students will:
EEN.RN.A. 2 Recognize the radical representation.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content Standards

## Number and Quantity - Quantities

Reason quantitatively and use units to solve problems. (C)
N.Q.C. 1 Use units as a way to understand problems and to guide the solution of multi-step problems; choose and interpret units consistently in formulas; choose and interpret the scale and the origin in graphs and data displays.
N.Q.C. 2 Define appropriate quantities for the purpose of descriptive modeling.
N.Q.C. 3 Choose a level of accuracy appropriate to limitations on measurement when reporting quantities.

## 2018 Wyoming Mathematics Content Standards

2020 Wyoming Math
Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## High School

EEN.Q.C.1-3 Choose and use an appropriate unit of measure to model and/or solve problems.

Level IV AA Students wiil:
EEN.Q.C.1-3 Choose and use an appropriate unit of measure to model and/or solve multi-step problems. Level III AA Students will: EEN.Q.C.1-3 Choose and use an appropriate unit of measure
to model and/or solve problems.
Level II AA Students will:
EEN.Q.C.1-3 dentify the attribute to be measured (e.g., weight, length, temperature) and select the appropriate unit of measure
Level : AA Students will:
EEN.Q.C.1-3 Identify measurement tools,

## 2020 Wyoming Math

 Extended Standardsinstructional Achievement Level Descriptor (ALDs)

## Number and Quantity - The Complex Number

 SystemPerform arithmetic operations with complex numbers. (D)
N.CN.D. 1 Know there is a complex number i such that $\mathrm{i}^{2}=-$

1 , and every complex number has the form $a+$ bi with $a$ and $b$ real.
N.CN.D. 2 Use the relation $i^{2}=-1$ and the commutative, associative, and distributive properties to add, subtract, and multiply complex numbers.
N.CN.D. 3 (+) STANDARD FOR ADVANCED COURSES

Represent complex numbers and their operations on the complex plane. (E)
N.CN.E.4-6 (+) STANDARD FOR ADVANCED COURSES
Use complex numbers in polynomial identities and equations. (F)
N.CN.F. 7 Solve quadratic equations with real coefficients that have complex solutions.

## N.CN.F.8-9 (+) STANDARD FOR ADVANCED COURSES

## High School

| EEN.CN.D.1 Not <br> applicabie. | ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this <br> standard that are appropriate for this population and/or <br> they have been covered in previous standards. |
| :--- | :--- |
| EEN.CN.D.2-3 Not <br> applicable. | ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this <br> standard that are appropriate for this population and/or <br> they have been covered in previous standards. |
| EEN.CN.E.4-6 Not <br> applicable. | ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this <br> standard that are appropriate for this population and/or <br> they have been covered in previous standards. |
| EEN.CN.F.7-9 Not <br> applicable. | ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this <br> standard that are appropriate for this population and/or <br> they have been covered in previous standards. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement level Descriptor (ALDs) |
| :---: | :---: | :---: |
| Number and Quantity - Vector and Matrix Quantities | High School |  |
| Represent and model with vector quantities. (G) N.VM.G.1-12 (+) STANDARD FOR ADVANCED COURSES | EEN.CN.D. 1 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDS) |
| Algebra - Seeing Structure in Expressions | High School |  |
| Interpret the structure of expressions. (A) <br> A.SSE.A. 1 Interpret expressions that represent a quantity in terms of its context. <br> A. Interpret parts of an expression, such as terms, factors, and coefficients. <br> B. Interpret complicated expressions by viewing one or more of their parts as a single entity. | EEA.SSE.A. 1 Identify the terms, factors, and coefficients related to expression. | Level IV AA Students will: <br> EEA.SSE.A. 1 Identify the terms, factors, and coefficients related to expressions within a context. <br> Level III AA Students will: <br> EEA.SSE.A. 1 Identify the terms, factors, and coefficients related to expressions. <br> Level II AA Students will: <br> EEA.SSE.A. 1 Determine the number of terms within an expression. <br> Level I AA Students will: <br> EEA.SSE.A. 1 Recognize that a coefficient is a number. |
| A.SSE.A. 2 Use the structure of an expression to identify ways to rewrite it. | EEA.SSE.A. 2 Write an equivalent expression involving a variable. | Level IV AA Students will: <br> EEA.SSE.A. 2 Demonstrate multiple ways to write an equivalent expression involving variables. <br> Level III AA Students will: <br> EEA.SSE.A. 2 Write an equivalent expression involving a variable. <br> Level II AA Students will: <br> EEA.SSE.A. 2 Write an equivalent expression. <br> Level I AA Students will: <br> EEA.SSE.A. 2 Identify an equivalent expression. |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Write expressions in equivalent forms to solve
problems. (B) problems. (B)
A.SSE.B. 3 Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.
A. Factor a quadratic expression to reveal the zeros of the function it defines.
B. Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.
C. Use the properties of exponents to transform expressions for exponential functions. Apply the concepts of decimal and scientific notation to solve real-world and mathematical problems.
i. Multiply and divide numbers expressed in both decimal and scientific notation.
ii. Add and subtract numbers in scientific notation with the same integer exponent.
A.SSE.B. 4 Derive the formula for the sum of a finite geometric series (when the common ratio is not 1 ), and use the formula to solve problems.

## 2018 Wyoming Mathematics Content Standards

## Algebra - Arithmetic with Polynomials and

## Rational Expressions

Perform arithmetic operations on polynomials. (C)
A.APR.C. 1 Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

EEA.SSE.B. 3 Given an equation in slopeintercept form, identify the constant as the $y$ intercept and coefficient as the slope of a line.

EEA.SSE.B. 4 Not applicable.

2020 Wyoming Math Extended Standards

Level IV AA Students will:
EEA.SSE.B. 3 Given an equation in slope-intercept form, identify the constant as the y-intercept and coefficient as the slope of a line, which may be increasing (positive), decreasing (negative), or constant (zero).
Level III AA Students will:
EEA.SSE.B. 3 Given an equation in slope-intercept form, identify the constant as the $y$-intercept and coefficient as the slope of a line.
Level II AA Students will:
EEA.SSE.B. 3 Given an equation in slope-intercept form, identify both the constant and coefficient.
Level I AA Students will:
EEA.SSE.B. 3 Given an equation in slope-intercept form, identify the constant.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Instructional Achievement Level Descriptor (ALDs)

## High School

EEA.APR.C. 1 Add and subtract polynomials.

Level IV AA Students will:
EEA.APR.C. 1 Add, subtract, and multiply polynomials. Level III AA Students will:
EEA.APR.C. 1 Add and subtract polynomials. Level II AA Students will:
EEA.APR.C. 1 Add polynomials.
Level I AA Students will:
EEA.APR.C. 1 Identify a polynomial, limited to monomial, binomial and trinomial.

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

Understand the relationship between zeros and factors of polynomials (D)
A.APR.D. 2 Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number a, the remainder on division by $x-a$ is $p(a)$, so $p(a)=0$ if and only if $(x-a)$ is a factor of $p(x)$. A.APR.D. 3 Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

Understand polynomial identities to solve problems (E)
A.APR.E. 4 Prove polynomial identities and use them to describe numerical relationships.

## A.APR.E. 5 (+) STANDARD FOR ADVANCED

 COURSES
## Rewrite rational expressions (F)

A.APR.F. 6 Rewrite simple rational expressions in different forms; write $a(x) / b(x)$ in the form $q(x)+r(x) / b(x)$, where $a(x)$, $b(x), q(x)$, and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$ using inspection, long division, or, for the more complicated examples, a computer algebra system. (e.g., rewriting a rational expression as the quotient plus the remainder over divisor).
A.APR.F. 7 (+) STANDARD FOR ADVANCED COURSES

## 2018 Wyoming Mathematics Content Standards

## Algebra - Creating Equations

Create equations that describe numbers or relationships. (G)
A.CED.G. 1 Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

EEA.APR.D.2-3 Not applicable.

EEA.APR.E.4-5 Not applicable.

EEA.APR.F.6-7 Not applicable.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
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## 2020 Wyoming Math

Extended Standards
Instructional Achievement Level Descriptor (ALDs)

## High School

EEA.CED.G. 1 Solve a one-step equation or inequality with one variable.

Level IV AA Students will:
EEA.CED.G. 1 Create and solve an equation or inequality with one variable.
Level III AA Students will:
EEA.CED.G. 1 Solve a one-step equation or inequality with one variable.
Level II AA Students will:
EEA.CED.G. 1 Solve a one-step equation with one variable.
Level I AA Students will:
EEA.CED.G. 1 Identify the variable within an equation.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

A.CED.G. 2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
A.CED.G. 3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context.
A.CED.G. 4 Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.

## 2018 Wyoming Mathematics Content Standards

## Algebra - Reasoning with Equations and

 InequalitiesUnderstand solving equations as a process of reasoning and explain the reasoning. (H)
A.REI.H. 1 Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.

EEA.CED.G. 2 Given an equation in slopeintercept form and its related table, graph a line.

## applicable.

Level IV AA Students will:
EEA.CED.G. 2 Given an equation in slope-intercept form, graph a line.
Level III AA Students will
EEA.CED.G. 2 Given an equation in slope-intercept form and its related table, graph a line
Level II AA Students will:
EEA.CED.G. 2 Given an equation in slope-intercept form and its related table, plot the y-intercept.
Level I AA Students will:
EEA.CED.G. 2 Recognize points in a table as ordered pairs ( $x$, y).
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## 2020 Wyoming Math Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## Hiah School

EEA.REI.H. 1 Show steps in solving a simple equation.

EEA.REI.H. 2 Not applicable.

EEA.REI.I. 3 Solve a two-step, linear equation in one variable.

## Level IV AA Students will: <br> EEA.REI.H. 1 Show steps and provide justification to a solution. Level III AA Students will: <br> EEA.REI.H. 1 Show steps in solving a simple equation. Level II AA Students will: <br> EEA.REI.H. 1 Identify the inverse operation needed to solve an equation. <br> Level I AA Students will: <br> EEA.REI.H. 1 Identify the operation within a simple equation. <br> ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. <br> Level IV AA Students will: <br> EEA.REI.I. 3 Solve a two-step, linear inequality in one variable, containing a positive, whole number coefficient. <br> Level III AA Students will: <br> EEA.REI.I. 3 Solve a two-step, linear equation in one variable.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

|  |  | Level II AA Students will: <br> EEA.REI.I. 3 Solve a one-step equation containing a whole number coefficient. (e.g., $15=3 x$ ) <br> Level I AA Students will: <br> EEA.REI.I. 3 Solve a one-step equation using addition or subtraction. (e.g., $5=\hat{x}+2$ ) |
| :---: | :---: | :---: |
| A.REI.I. 4 Solve quadratic equations in one variable. <br> A. Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form $(x-p)^{2}=q$ that has the same solutions. <br> B. Solve quadratic equations by inspection (e.g., for $x^{2}=$ 49), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$. <br> C. (+) Derive the quadratic formula from the general form of a quadratic equation. | EEA.REI.I. 4 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| Solve systems of equations (J) <br> A.REI.J. 5 Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions. | EEA.REI.J. 5 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| A.REI.J. 6 Estimate solutions graphically and determine algebraic solutions to linear systems, focusing on pairs of linear equations in two variables. | EEAREI. $\mathbf{3 . 6}$ Locate the solution to a system of linear equations by naming the point of intersection. | Level IV AA Students will: <br> EEA.REI.J. 6 Create two intersecting lines and estimate the point of intersection. <br> Level III AA Students will: <br> EEA.REI.J. 6 Locate the solution to a system of linear <br> equations by naming the point of intersection. (e.g., a graph showing two lines that intersect) <br> Level II AA Students will: <br> EEA.REI.J. 6 Locate both the $x$ - and $y$ - axes on a graph. <br> Level I AA Students will: <br> EEA.REI.J. 6 Locate the intersection of the $x$ - and $y$ - axes. |
| A.REI.J. 7 Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. <br> A.REI.J.8-9 (+) STANDARD FOR ADVANCED COURSES | EEA.REI.J.7-9 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| Represent and solve equations and inequalities graphically. (K) | EEA.REI.K. 10 Identify a solution to a linear equation, represented | Level IV AA Students will: EEA.REI.K. 10 Create a line and name multiple solutions. |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

A.REI.K. 10 Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane.
A.REI.K. 11 Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.
A.REI.K. 12 Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.

## 2018 Wyoming Mathematics Content Standards

## Functions - Interpreting Functions

Understand the concept of a function and use function notation. (A)
F.IF.A. 1 Understand that a function from one set (called the domain) to another set (called the range) assigns to each element of the domain exactly one element of the range. If $f$ is a function and $x$ is an element of its domain, then $f(x)$ denotes the output of $f$ corresponding to the input $x$. The graph of $f$ is the graph of the equation $y=f(x)$.
F.IF.A. 2 Use function notation, evaluate functions for inputs in their domains, and interpret statements that use function notation in terms of a context.
F.IF.A. 3 Recognize that sequences are functions, sometimes defined recursively, whose domain is a subset of the integers.
Interpret functions that arise in applications in terms
graphically as a line.
Level III AA Students will:
EEA.REI.K. 10 Identify a solution to a linear equation, represented graphically as a line.
(e.g., given a line and a point on the line, identify the solution)

Level II AA Students will:
EEA.REI.K. 10 Locate both the $x$ - and $y$ - axes.
Level I AA Students will:
EEA.REI.K. 10 Locate a point on a line.
EEA.REI.K.11-12 Not applicable.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

of the context. (B)
F.IF.B. 4 For a function that models a relationship between two quantities, interpret key features of graphs and tables in terms of the quantities, and sketch graphs showing key features given a verbal description of the relationship. Key features include: intercepts; intervals where the function is increasing, decreasing, positive, or negative; relative maximums and minimums; symmetries; end behavior; and periodicity.
F.IF.B. 5 Relate the domain of a function to its graph and, where applicable, to the quantitative relationship it describes. F.IF.B. 6 Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.

## Analyze functions using different representations.

 (C)F.IF.C. 7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
A. Graph linear and quadratic functions and show intercepts, maxima, and minima.
B. Graph square root, cube root, and piecewise-defined functions, including step functions and absolute value functions.
C. Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior.
D. (+) STANDARD FOR ADVANCED COURSES
E. Graph exponential and logarithmic functions, showing intercepts and end behavior.
F. (+) STANDARD FOR ADVANCED COURSES
F.IF.C. 8 Write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function.
A. Use the process of factoring and completing the square in a quadratic function to show zeros, extreme
function, interpret key features of a graph and/or table, including whether the function is increasing, decreasing, or constant.

## EEF.IF.B.5-6 Not

 applicable.
## EEF.IF.C. 7 Not

 applicable.EEF.IF.B. 4 Interpret key features of a graph and/or table, which may include intercepts and/or intervals.
Level III AA Students will:
EEF.IF.B. 4 For a function, interpret key features of a graph and/or table, including whether the function is increasing, decreasing, or constant.
Level II AA Students wiil:
EEF.IF.B. 4 Using a graph, identify whether a function is increasing, decreasing, or constant.
Level I AA Students will:
EEF.IF.B. 4 Using a graph, recognize whether a function is increasing.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

values, and symmetry of the graph, and interpret these in terms of a context.
B. Use the properties of exponents to interpret expressions for exponential functions.
F.IF.C. 9 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

## 2018 Wyoming Mathematics Content Standards

## Functions - Building Functions

Build a function that models a relationship between two quantities. (D)
F.BF.D. 1 Write a function that describes a relationship between two quantities
A. Determine an explicit expression, a recursive process, or steps for calculation from a context.
B. Combine standard function types using arithmetic operations.
C. (+) Compose functions. For example, if $T(y)$ is the temperature in the atmosphere as a function of height, and $h(t)$ is the height of a weather balloon as a function of time, then $T(h(t))$ is the temperature at the location of the weather balloon as a function of time.
F.BF.D. 2 (+) Write arithmetic and geometric sequences both recursively and with an explicit formula, use them to model situations, and translate between the two forms. (+)

## STANDARD FOR ADVANCED COURSES

## Build new functions from existing functions. (E)

F.BF.E. 3 Identify the effect on the graph of replacing $f(x)$ by $f(x)+k, k f(x), f(k x)$, and $f(x+k)$ for specific values of $k$ (both positive and negative); find the value of $k$ given the graphs. Experiment with cases and illustrate an explanation of the effects on the graph using technology. Include recognizing even and odd functions from their graphs and algebraic expressions for them.
F.BF.E. 4 Find inverse functions.
A. Write an expression for the inverse of a simple, invertible function $f(x)$. Understand that an inverse function can be obtained by expressing the dependent variable of one function as the independent variable of

EEF.IF.C. 9 Not applicable.

## 2020 Wyoming Math

 Extended Standards***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Instructiona: Achievement Level Descriptor (ALDs)

## High School

## EEF.BF.D. 1 Match a

function that describes a relationship between the input and output, within a context

Level IV AA Students will:
EEFBF.D. 1 Write a function that describes the relations, within a context.
Level III AA Students will:
EEF.BF.D. 1 Match a function that describes a relationship
between the input and output, within a context.
Level II AA Students will:
EEF.BF.D. 1 Describe how the input and output are related. Level I AA Students will:
EEF.BF.D. 1 Identify key information.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

another, as $f$ and $g$ are inverse functions, if and only if, $f(x)=y$ and $g(y)=x$, for all values of $x$ in the domain of $f$ and all values of $y$ in the domain of $g$.
B. (+) Verify by composition that one function is the inverse of another.
C. (+) Read values of an inverse function from a graph or a table, given that the function has an inverse.
D. (+) Produce an invertible function from a non-invertible function by restricting the domain.
F.BF.E. 5 (+) STANDARD FOR ADVANCED COURSES

## 2018 Wyoming Mathematics Content Standards

2020 Wyoming Math
Extended Standards
Instructiona! Achievement Level Descriptor (ALDs)

## Functions - Linear, Quadratic, and Exponential Models

Construct and compare linear, quadratic, and exponential models and solve problems. (F)
F.LE.F. 1 Distinguish between situations that can be modeled with linear functions and with exponential functions.
A. Verify that linear functions grow by equal differences over equal intervals and that exponential functions grow by equal factors over equal intervals.
B. Recognize situations in which one quantity changes at a constant rate per unit interval relative to another.
C. Recognize situations in which a quantity grows or decays by a constant percent rate per unit interval relative to another
F.LE.F. 2 Construct linear and exponential functions using a graph, a description of a relationship, or two input-output pairs (include reading these from a table).
F.LE.F. 3 Observe using graphs and tables that a quantity increasing exponentially eventually exceeds a quantity increasing linearly, quadratically, or (more generally) as a polynomial function.

## High School

## EEF.LE.F. 1 Not

 applicable.***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

F.LE.F. 4 For exponential models, express as a logarithm the solution to $a b^{(c t)}=d$ where $a, c$, and $d$ are numbers and the base $b$ is 2,10 , or $e$; evaluate the logarithm using technology
F.LE.F. 5 Interpret the parameters in a linear or exponential function in terms of a context.

2018 Wyoming Mathematics Content Standards

## Functions - Trigonometric Functions

F.TF.H. 1 - F.TFJ. 9
(+) STANDARD FOR ADVANCED COURSES

## 2018 Wyoming Mathematics Content Standards

## Geometry - Congruence

Experiment with transformations in the plane. (A) G.CO.A. 1 Apply precise definitions of angle, circle, perpendicular line, parallel line, and line segment, based on the undefined notions of point, line, distance along a line, and distance around a circular arc.
G.CO.A. 2 Represent transformations in the plane using, e.g., transparencies and geometry software; describe transformations as functions that take points in the plane as inputs and give other points as outputs. Compare transformations that preserve distance and angle to those that do not (e.g., translation versus horizontal stretch).
G.CO.A. 3 Given a rectangle, paralielogram, trapezoid, or regular polygon, describe the rotations and reflections that carry it onto itself.

EEF.LE.F. 5 Not $\quad$ ***The Extended Standards Educator Committee applicable.

2020 Wyoming Math Extended Standards determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Instructional Achievement Level Descriptor (ALDs)

## High School

EEF.TF.H.1-9 Not applicable.

## 2020 Wyoming Math Extended Standards

## High School

EEG.CO.A. 1 Recognize perpendicular lines, parallel lines, and line segments, angles, and circles.

EEG.CO.A. 2 Not applicable.

EEG.CO.A. 3 Not applicable.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population.

Instructional Achievement Level Descriptor (ALDs)

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

G.CO.A. 4 Develop definitions of rotations, reflections, and translations in terms of angles, circles, perpendicular lines, parallel lines, and line segments.
G.CO.A. 5 Given a geometric figure and a rotation, reflection, or translation, draw the transformed figure using, e.g., graph paper, tracing paper, or geometry software. Specify a sequence of transformations that will carry a given figure onto another.

EEG.CO.A.4-5
Recognize rotations, reflections, and translations.
they have been covered in previous standards.

## Level IV AA Students will:

EEG.CO.A.4-5 Recognize and/or demonstrate a combination of simple rotations, reflections, and translations.
Level III AA Students will:
EEG.CO.A.4-5 Recognize rotations, reflections, and translations.
Level II AA Students will:
EEG.CO.A.4-5 Match a geometric figure with its rotation, reflection, or translation.
Level I AA Students will:
EEG.CO.A.4-5 Identify a rotation, reflection, or translation for an object which is moved.
EEG.CO.B. 6 Recognize
that rigid
transformations maintain congruence

EEG.CO.B.7-8 Not
applicable.
motions to show that two triangles are congruent if and only corresponding pairs of sides and corresponding pairs of angles are congruent.
G.CO.B. 8 Explain how the criteria for triangle congruence (ASA, SAS, and SSS) follow from the definition of congruence in terms of rigid motions.

## Prove geometric theorems. (C)

G.CO.C. 9 Prove theorems about lines and angles. Theorems include: vertical angles are congruent; when a transversal crosses parallel lines, alternate interior angles are congruent and corresponding angles are congruent: points on a perpendicular bisector of a line segment are exactly those equidistant from the segments endpoints.
G.CO.C. 10 Prove theorems about triangles. Theorems include: measures of interior angles of a triangle sum to 180 degrees; base angles of isosceles triangles are congruent; the

Level IV AA Students will:
EEG.CO.B. 6 Demonstrate that using multiple rigid transformations maintain congruency.
Level III AA Students will:
EEG.CO.B. 6 Recognize that rigid transformations maintain congruency.
Level II AA Students will:
EEG.CO.B. 6 Identify congruent parts from its pre-image to image.
Level I AA Students will:
EEG.CO.B.6-Match shapes that are congruent.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

segment joining midpoints of two sides of a triangle is parallel to the third side and half the length; the medians of a triangle meet at a point.
G.CO.C. 11 Prove theorems about parallelograms. Theorems include: opposite sides are congruent, opposite angles are congruent, the diagonals of a parallelogram bisect each other, and conversely, rectangles are parallelograms with congruent diagonals.
Make geometric constructions. (D)
G.CO.D. 12 Make formal geometric constructions with a variety of tools and methods (compass and straightedge, string, reflective devices, paper folding, dynamic geometric software, etc.). Copying a segment; copying an angle; bisecting a segment; bisecting an angle; constructing perpendicular lines, including the perpendicular bisector of a line segment; and constructing a line parallel to a given line through a point not on the line.
G.CO.D. 13 Construct an equilateral triangle, a square, and a regular hexagon inscribed in a circle.

## EEG.CO.D.12. Create

 geometric figures using tools (e.g., ruler, protractor, compass and straightedge, string,reflective devices, paper folding, dynamic geometric software).

Level IV AA Students will:
EEG.CO.D. 12 Construct a geometric figure using mathematical tools.
Level III AA Students will:
EEG.CO.D. 12 Create geometric figures using tools (e.g., ruler, protractor, compass and straightedge, string, reflective devices, paper folding, dynamic geometric software).
Level II AA Students will:
EEG.CO.D.12. Create geometric figures without tracing. Level I AA Students will:
EEG.CO.D. 12 Trace geometric figures.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

## Geometry - Similarity, Right Triangles, and Trigonometry

Understand similarity in terms of similarity transformations. (E)
G.SRT.E. 1 Understand similarity in terms of similarity transformations. Verify heuristically the properties of dilations given by a center and a scale factor.
A. A dilation takes a line not passing through the center of the dilation to a parallel line, and leaves a line passing through the center unchanged.
B. The dilation of a line segment is longer or shorter in the ratio given by the scale factor.
G.SRT.E. 2 Given two figures, use the definition of similarity in terms of similarity transformations to decide if they are similar; explain using similarity transformations the meaning of similarity for triangles as the equality of all corresponding pairs of angles and the proportionality of all corresponding pairs of sides.
G.SRT.E. 3 Use the properties of similarity transformations to establish the AA criterion for two triangles to be similar

## Prove theorems involving similarity. (F)

G.SRT.F. 4 Prove theorems about triangles. Theorems include: a line parallel to one side of a triangle divides the other two proportionally, and conversely; the Pythagorean Theorem proved using triangle similarity.
G.SRT.F. 5 Use congruence and similarity criteria for triangles to solve problems and to prove relationships in geometric figures.
Define trigonometric ratios and solve problems involving fight triangles. (G)
G.SRT.G. 6 Understand that by similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles.
G.SRT.G. 7 Explain and use the relationship between the sine and cosine of complementary angles.
G.SRT.G. 8 Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.
G.SRT.H.9-11 (+) STANDARD FOR ADVANCED COURSES

2020 Wyoming Math $\quad$ Instructional Achievement Level Extended Standards Descriptor (ALDs)

## High School

EEG.SRT.E.1-3 Not applicable.
***The Extended Standards Educator Committee determined there are no real-worid applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
applicable.

EEG.SRT.G.6-11 Not applicable.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## 2018 Wyoming Mathematics Content Standards

## Geometry - Circles

Understand and apply theorems about circles. (I)
G.C.I. 1 Prove that all circles are similar.
G.C.I. 2 Identify and describe relationships among inscribed angles, radii, and chords. Include the relationship between central, inscribed, and circumscribed angles; inscribed angles on a diameter are right angles; the radius of a circle is perpendicular to the tangent where the radius intersects the circle.
G.C.I. 3 Construct the inscribed and circumscribed circles of a triangle, and prove properties of angles for a quadrilateral inscribed in a circle
G.C.I. 4 (+) Construct a tangent line from a point outside a given circle to the circle.
Find arc lengths and areas of sectors of circles. (J)
G.C.J. 5 Derive using similarity the fact that the length of the arc intercepted by an angle is proportional to the radius, and define the radian measure of the angle as the constant of proportionality; derive the formula for the area of a sector.

## 2018 Wyoming Mathematics Content Standards

Geometry - Expressing Geometric Properties with Equations
Translate between the geometric description and the equation for a conic section. (K)
G.GPE.K. 1 Derive the equation of a circle of given center and radius using the Pythagorean Theorem; complete the square to find the center and radius of a circle given by an equation.

## G.GPE.K.2-3 (+) STANDARD FOR ADVANCED

## COURSES

Use coordinates to prove simple geometric theorems algebraically. (L)

2020 Wyoming Math
Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## High School

EEG.C.I.1-2 Identify properties of circles, including center, diameter, radius, circumference, chord, and central angles.

Level IV AA Students will:
EEG.C.I.1-2 Use a property of circles to describe how circles are similar.

## Level III AA Students will:

EEG.C.I.1-2 Identify properties of circles, including center, diameter radius, circumference, chord, and central angles.

Level II AA Students will:
EEG.C.1-2 Identify properties of circles, including center, diameter, radius, and circumference
Level I AA Students will:
EEG.C.I.1-2 Identify circles both as representations and in real life applications.
EEG.C.I.3-4. Not **The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## 2020 Wyoming Math

 Extended StandardsInstructional Achievement Level Descriptor (ALDs)

## High School

| EEG.GPE.K.1-3 Not <br> applicable. | $* * *$ The Extended Standards Educator Committee <br> determined there are no real-world applications for this <br> standard that are appropriate for this population and/or <br> they have been covered in previous standards. |
| :--- | :--- |
| EEG.GPE.L.4 Not <br> applicable. | ***The Extended Standards Educator Committee <br> determined there are no real-world applications for this |

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## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

G.GPE.L. 4 Use coordinates to prove simple geometric theorems algebraically.
G.GPE.L. 5 Prove the slope criteria for parallel and perpendicular lines and use them to solve geometric problems (e.g., find the equation of a line parallel or perpendicular to a given line that passes through a given point).
G.GPE.L. 6 Find the point on a directed line segment between two given points that partitions the segment in a given ration.
G.GPE.L. 7 Use coordinates to compute perimeters of polygons and areas of triangles and rectangles, (e.g., using the distance formula).

## 2018 Wyoming Mathematics Content Standards

## Geometry - Geometric Measurement and

Dimension
Explain volume formulas and use them to solve problems. (M)
G.GMD.M. 1 Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone. Use dissection arguments, Cavalieri's principle, and informal limit arguments.
G.GMD.M. 2 (+) Give an informal argument using Cavalieri's Principle for the formulas for the volume of a sphere and other solid figures.
standard that are appropriate for this population and/or they have been covered in previous standards.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

Level IV AA Students will:
EEG.GPE.L. 7 Caiculate the perimeter and area of squares and rectangles to solve real-world problems.
Level III AA Students will:
EEG.GPE.L. 7 Provided formulas and measurements,
calculate the perimeter and area of squares and rectangles to solve real-world problems.
Level II AA Students will:
EEG.GPE.L. 7 Find perimeter or area by counting on a grid.

## Level I AA Students will:

EEG.GPE.L. 7 On a grid, identify the inside of a figure as the area and edges of a figure as the perimeter.

## 2020 Wyoming Math

Extended Standards
Instructional Achievement Level Descriptor (ALDs)

## High School

EEG.GMD.M.1-2 Not applicable.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| G.GMD.M. 3 Use volume formulas for cylinders, pyramids, cones, and spheres to solve problems. | EEG.GMD.M. 3 Provided formulas and measurements, calculate the volume of three dimensional objects including cubes, rectangular prisms, cylinders, spheres, or cones to solve realworld problems. | Level IV AA Students will: <br> EEG.GMD.M. 3 Provided formulas and measurements, predict volumes of non-similar, three-dimensional objects and verify the prediction through calculation. <br> Level III AA Students vill: <br> EEG.GMD.M. 3 Provided formulas and measurements, calculate the volume of three dimensional objects including cubes, rectangular prisms, cylinders, spheres, or cones to solve real-world problems. <br> Level II AA Students will: <br> EEG.GMID.M. 3 Using two similar, three-dimensional objects, predict which has a greater volume and verify the prediction. (e.g., fill containers with water, rice, use a formula). <br> Level I AA Students will: <br> EEG.GMD.M. 3 Match the three-dimensional object with its appropriate math term. |
| :---: | :---: | :---: |
| Visualize relationships between two-dimensional and three-dimensional objects. (N) <br> G.GMD.N. 4 Identify the shapes of two-dimensional crosssections of three-dimensional objects, and identify threedimensional objects generated by rotations of two-dimensional object. | EEG.GMD.N. 4 Identify the shapes of twodimensional crosssections of threedimensional objects. | Level IV AA Students will: <br> EEG.GMD.N. 4 Identify multiple shapes within two- <br> dimensional cross-sections of three-dimensional objects. <br> Level III AA Students will: <br> EEG.GMD.N. 4 Identify the shapes within two-dimensional cross-sections of three-dimensional objects. <br> Level II AA Students will: <br> EEG.GMD.N. 4 Identify the two-dimensional bases of threedimensional objects. <br> Level I AA Students will: <br> EEG.GMD.N.4. Identify two-dimensional versus three- <br> dimensional shapes. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

2018 Wyoming Mathematics Content
Standards

## Geometry - Modeling with Geometry

Apply geometric concepts in modeling situations. (O)
G.MG.O.1 Use geometric shapes, their measures, and their properties to describe objects (e.g., modeling a tree trunk or a human torso as a cylinder).
G.MG.O. 2 Apply concepts of density based on area and volume in modeling situations (e.g., persons per square mile, BTUs per cubic foot).
G.MG.O. 3 Apply geometric methods to solve design problems (e.g., designing an object or structure to satisfy physical constraints or minimize cost; working with typographic grid systems based on ratios).

## 2018 Wyoming Mathematics Content

 StandardsStatistics and Probability - Interpreting Categorical and Quantitative Data
Summarize, represent, and interpret data on a single count or measurement variable. (A)
S.ID.A. 1 Represent data with plots on the real number line (dot plots, histograms, and box plots) by hand or using technology.


2020 Wyoming Math
Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## High School

EEG.MG.O.1 Describe
real-life items using geometric shapes or objects.

## Level IV AA Students will:

EEG.MG.O.1 Create a real-life item composed of geometric shapes or objects and describe its geometric parts.
Level III AA Students will:

EEG.MG.O.1 Describe real-life items using geometric shapes or objects.
Level II AA Students will:
EEG.MG.O. 1 Describe characteristics of three-dimensional geometric objects.
Level I AA Students will:
EEG.MG.O.1 Identify two-dimensional geometric shapes.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## 2020 Wyoming Math <br> Extended Standards

Instructional Achievement Level Descriptor (ALDs)

## High School

EES.ID.A. 1 Match the given data to its graphical
representation, which may include dot plots bar graphs, or pie charts.

Level IV AA Students will:
EES.ID.A. 1 Given data, construct a simple graph, such as a dot plot, bar graph, or pie chart.
Level III AA Students will:
EES.ID.A. 1 Match the given data to its graphical representation, which may include dot plots, bar graphs, or pie charts.
Level II AA Students will:
EES.ID.A. 1 Identify the type of graph.
Level I AA Students will:
EES.ID.A. 1 Identify the parts of a simple graph.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

S.ID.A. 2 Use statistics appropriate to the shape of the data distribution to compare center (median, mean) and spread (interquartile range, standard deviation) of two or more different data sets.
S.ID.A. 3 Interpret differences in shape, center, and spread in the context of the data sets, accounting for possible effects of extreme data points (outliers).
S.ID.A. 4 (+) Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimate population percentages. Recognize that there are data sets for which such a procedure is not appropriate. Use the Empirical Rule, calculators, spreadsheets, and/or tables to estimate areas under the normal curve.
Summarize, represent, and interpret data on two categorical and quantitative variables. (B)
S.ID.B. 5 (+) Summarize categorical data for two categories in two-way frequency tables. Interpret relative frequencies in the context of the data (including joint, marginal, and conditional relative frequencies). Recognize possible associations in the data, and use inferential statistical techniques to show association.
S.ID.B. 6 Represent data on two quantitative variables on a scatter plot, and describe how the variables are related.
A. Use a function to describe data trends to solve problems in the context of the data Use given functions or choose a function suggested by the context. Emphasize linear, quadratic, and exponential models.
B. (+) Informally assess the fit of a function by plotting and analyzing residuals.
C. Using technology, fit a least squares linear regression function for a scatter plot that suggests a linear association.

EES.ID.A.2-3 Given a
graph, determine measures of central tendency, which may include mean, median, mode, or other measures such as range or outliers.

EES.ID.A. 4 Not applicable.

EES.ID.B.5.
Not applicable.

## EES.ID.B. 6 Given

multiple linear trendlines, determine which one best represents the data.

Level IV AA Students will:
EES.ID.A.2-3 Given a graph or data, describe how an outlier would impact any measure of central tendency.

## Level III AA Students will:

EES.ID.A.2-3 Given a graph or data, determine measures of central tendency, which may include mean, median, mode, or other measures such as range or outliers.
Level II AA Students will:
EES.ID.A.2-3 Given a graph or data, determine the mean or median.
Level I AA Students will.
EES-ID.A.2-3 Given a graph or data, determine the mode.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.
***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards.

## Level IV AA Students will:

EES.ID.B. 6 Given a scatter plot, place a linear trendline and justify its placement.
Level III AA Students will:
EES.ID.B. 6 Given multiple linear trendlines, determine which one best represents the data.
Level II AA Students will:
EES.ID.B. 6 Differentiate between a scatter plot that is increasing versus decreasing.
Level I AA Students will:
EES.ID.B. 6 Identify a scatter plot that is increasing.

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

| Interpret linear models. (C) <br> S.ID.C. 7 Interpret the slope (rate of change) and the intercept (constant term) of a linear model in the context of the data. | EES.ID.C. 7 <br> Given a graph, identify the slope as increasing (positive), decreasing (negative), or constant (zero) and find the $y$ intercept. | Level IV AA Students will: <br> EES.ID.C. 7 Given a graph, interpret the slope or y-intercept within a context. <br> Level III AA Students will: <br> EES.ID.C. 7 Given a graph, identify the slope as increasing (positive), decreasing (negative), or constant (zero) and find the y-intercept. <br> Level II AA Students will: <br> EES.ID.C. 7 Identify the $y$-intercept as the point where a line intersects the $y$-axis. <br> Level I AA Students will: <br> EES.ID.C. 7 Identify the slope of a line as increasing (positive) or decreasing (negative). |
| :---: | :---: | :---: |
| S.ID.C. 8 Compute (using technology) and interpret the correlation coefficient of a linear fit. <br> S.ID.C. 9 Distinguish between correlation and causation. | EES.ID.C.8-9 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| 2018 Wyoming Mathematics Content Standards | 2020 Wyoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Statistics and Probability - Making Inferences and Justifying Conclusions | High School |  |
| Understand and evaluate random processes underlying statistical experiments. (D) S.IC.D.1-6 (+) STANDARD FOR ADVANCED COURSES | EES.IC.D.1-6 Not applicable. | ***The Extended Standards Educator Committee determined there are no real-world applications for this standard that are appropriate for this population and/or they have been covered in previous standards. |
| 2018 Wyoming Mathematics Content Standards | 2020 Myoming Math Extended Standards | Instructional Achievement Level Descriptor (ALDs) |
| Statistics and Probability - Conditional Probability and the Rules of Probability | High School |  |
| Understand independence and conditional probability and use them to interpret data. (F) <br> S.CP.F. 1 Describe events as subsets of a sample space (the set of outcomes) using characteristics (or categories) of the outcomes, or as unions, intersections, or complements of other events ("or," "and," "not"). <br> S.CP.F.2-4 (+) STANDARD FOR ADVANCED COURSES | EES.CP.F. 1 List the possible outcomes of an event. | Level IV AA Students will: <br> EES.CP.F. 1 Compare theoretical and experimental outcomes. <br> Level III AA Students will: <br> EES.CP.F. 1 List the possible outcomes of an event. <br> Level II AA Students will: <br> EES.CP.F. 1 Identify the chance of an event as more, less, or equally likely. <br> Level I AA Students will: <br> EES.CP.F. 1 Identify the chance of an event as impossible, possible, or certain. |

## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS



## DRAFT 2020 WYOMING MATH EXTENDED STANDARDS AND ACHIEVEMENT LEVEL DESCRIPTORS

## High School Mathematics Standards

NOTE: This table shows the Advanced Level Standards that are designated with $a(+)$ in the general education Math Standards, which were not included in the Extended Standards The (t) standards are designated for complex, advanced-level math courses.

| 2018 Math Standard Code(s) | Cluster Heading |
| :--- | :--- |
| T.CN.3-6, 8-9 | Vector \& Matrix Quantities |
| N.VM.1-12 | Arithmetic with Polynomial \& Rational Expressions |
| A.APR.5\&7 | Reasoning with Equalities and Inequalities |
| A.REI.8-9 | Interpreting Functions |
| F.IF.7d | Building Functions |
| F.BF.1c, 2, 4b-d, 5 | Trigonometric Functions |
| F.TF.1-9 | Similarities, Right Triangles, \& Trigonometry |
| G.SRT.9-11 | Circles |
| G.C.4 | Geometric Measurement \& Dimension |
| G.GMD.2 | Interpreting Categorical and Quantitative Data |
| S.ID.4-5 \& 6b | Making Inferences and Justifying Conclusions |
| S.IC.1-6 | Conditional Probability \& the Rules of Probability |
| S.CP.2-4 \& 6-9 | Using Probability to Make Decisions |
| S.MD.1-7 |  |

