

| Level   | Basic  | Proficient  | Advanced   |
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| <b>Policy Level Descriptors</b>   | Marginal academic performance, work approaching, but not yet reaching, satisfactory performance, indicating partial understanding and limited display of the knowledge and skills included in the Wyoming Content and Performance Standards. | Satisfactory academic performance indicating a solid understanding and display of the knowledge and skills included in the Wyoming Content and Performance Standards. | Superior academic performance indicating an in-depth understanding and exemplary display of the knowledge and skills included in the Wyoming Content and Performance Standards.      |
| <b>Domain</b>   | <b>The Number System</b>   |   |  |
| <b>Range PLD: Cluster A</b> - Know that there are numbers that are not rational and approximate them by rational numbers. | Basic students identify numbers as being rational or irrational (8.NS.1);  |   |  |
|   |  | Proficient students determine the repeating decimal expansion for a rational number and determine the rational number from a repeating decimal expansion (8.NS.1);    |  |
|   |  | Proficient students determine that a non-repeating decimal expansion represents an irrational number (8.NS.2).  | Advanced students use approximation strategies with rational numbers to identify and compare the estimated values of irrational numbers with respect to a real number line (8.NS.2). |

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| <b>Domain</b>  | <b>Expressions and Equations</b>  |   |   |
| <b>Range PLD: Cluster B -</b><br>Work with radicals and integer exponents.   | Basic students apply the properties of integer exponents with only positive integers involving one operation (8.EE.1);  | Proficient students apply the properties of integer exponents with integers to generate equivalent numerical expressions (8.EE.1);  | Advanced students apply the properties of integer exponents with integers involving multiple negative exponents (8.EE.1);   |
|  | Basic students represent solutions with either square root or cube root symbols for $x$ in the equations $x^2 = p$ and $x^3 = p$ when $p$ is a whole number (8.EE.2); | Proficient students represent solutions with both square root and cube root symbols for $x$ in the equations $x^2 = p$ and $x^3 = p$ when $p$ is a positive rational number (8.EE.2);   | Advanced students represent solutions of two-step equations with both square root and cube root symbols for $x$ in the equations $x^2 + a = p$ and $x^3 + a = p$ when $a$ and $p$ are rational numbers and $p - a$ is greater than 0;                   |
|  |   | Proficient students evaluate square roots of perfect squares up to 144 and cube roots of perfect cubes up to 1,000 (8.EE.2);  |   |
|  | Basic students express numbers in scientific notation (8.EE.3).   | Proficient students compare or multiply/divide two numbers in scientific notation (8.EE.4);   | Advanced students compare or apply the four operations (+, -, $\times$ , and $\div$ ) between two or more numbers in scientific notation (8.EE.4).  |
|  |   | Proficient students choose units of appropriate size for measurements of very large or very small quantities in scientific notation (8.EE.4).   |   |
| <b>Range PLD: Cluster C -</b><br>Understand the connections between proportional relationships, lines, and linear equations. | Basic students graph proportional relationships from a table of values (8.EE.5);  | Proficient students graph proportional relationships from the equation $y = mx$ (8.EE.5);   | Advanced students compare two different proportional relationships represented in different ways (8.EE.5);  |
|  |   | Proficient students interpret the unit rate within context as the slope of the graph (8.EE.5);  | Advanced students explain why the slope ( $m$ ) is equivalent between any two different points located on any non-vertical line in the coordinate plane (8.EE.5);   |
|  | Basic students derive the equation $y = mx$ with slope ( $m$ ) from a graph (8.EE.6).   | Proficient students derive the equation $y = mx$ with slope ( $m$ ) from a table or graph and derive the equation $y = mx + b$ with slope ( $m$ ) and $y$ -intercept ( $b$ ) from a table or graph (8.EE.6).                                      | Advanced students derive the equation $y = mx + b$ with slope ( $m$ ) and $y$ -intercept ( $b$ ) from a verbal description (8.EE.6).  |
| <b>Range PLD: Cluster D -</b><br>Analyze and solve linear equations and pairs of simultaneous linear equations.              | Basic students solve two-step linear equations in one variable with integer coefficients and constants (8.EE.7);  | Proficient students solve linear equations in one variable with integer coefficients and constants that require multi-steps and identify the solution of a linear equation in one variable as infinitely many solutions or no solutions (8.EE.7); | Advanced students solve linear equations in one variable with rational number coefficients and constants that require multi-steps and identify the solution of a linear equation in one variable as infinitely many solutions or no solutions (8.EE.7); |
|  | Basic students identify the solution to a system of two linear equations from a graph as the point of intersection of the two lines (8.EE.8).                         | Proficient students solve systems of two linear equations in two variables algebraically or graphically (8.EE.8).   | Advanced students construct and solve systems of two linear equations which represent real-world or mathematical problems (8.EE.8).   |

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| <b>Domain</b>   | <b>Functions</b>   |  |  |
| <b>Range PLD: Cluster E -</b><br>Define, evaluate, and compare functions.                 | Basic students evaluate functions with integer coefficients and constants with positive integers as the inputs (8.F.1);      | Proficient students evaluate functions with rational coefficients and constants with integers as the inputs (8.F.1);                                 | Advanced students evaluate functions with rational coefficients and constants with rational numbers as the inputs (8.F.1);                         |
|   |  | Proficient students identify if a table of values or a graph in the coordinate plane represent a function (8.F.1);                                   |  |
|   | Basic students compare the properties of two linear functions represented by graphs (8.F.2);                                 | Proficient students compare the properties of two linear functions represented in different ways (8.F.2);  | Advanced students compare the properties of two functions, with at least one non-linear function, which are represented in different ways (8.F.2); |
|   | Basic students identify linear and non-linear functions represented by graphs (8.F.3).                                       | Proficient students identify linear and non-linear functions represented by equations and tables (8.F.3).  | Advanced students identify linear and non-linear functions represented by verbal descriptions (8.F.3).   |
| <b>Range PLD: Cluster F -</b><br>Use functions to model relationships between quantities. | Basic students construct a graph to model a real-world linear relationship between two quantities (8.F.4);                   | Proficient students create an equation to represent a function which models a real-world linear relationship between two quantities (8.F.4);         | Advanced students use the graph and equation representing a function to analyze the relationship between two quantities (8.F.4);                   |
|   | Basic students determine the rate of change and initial value of a function from a graph (8.F.4);                            | Proficient students determine the rate of change and initial value of a function from a table (8.F.4);   | Advanced students determine the rate of change and initial value of a function from a verbal description (8.F.4);                                  |
|   | Basic students interpret the rate of change and initial value of a real-world linear function in terms of its graph (8.F.4); | Proficient students interpret the rate of change and initial value of a real-world linear function in terms of its graph or table of values (8.F.4); | Advanced students interpret the rate of change and initial value of a real-world linear function in terms of a verbal description (8.F.4);         |
|   | Basic students identify graphs of functional relationships as being linear or non-linear (8.F.5).                            | Proficient students identify and describe the qualitative features from analyzing a linear function (8.F.5).   | Advanced students identify and describe the qualitative features from analyzing a non-linear function (8.F.5).                                     |

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| <b>Domain</b>  | <b>Geometry</b>   |   |   |
| <b>Range PLD: Cluster G -</b><br>Understand congruence and similarity using physical models, transparencies, or geometry software. | Basic students identify the transformations (rotation, reflection, and translation) of figures (8.G.1);                     | Proficient students describe the effects on lines, line segments, and angles of figures when rotations, reflections, and translations are performed (8.G.1);  |   |
|  |   | Proficient students describe the properties of congruency between two figures when at most two transformations are performed (8.G.2);                         | Advanced students describe the properties of congruency between two figures when three or more transformations are performed (8.G.2);   |
|  | Basic students translation is performed on the coordinate plane (8.G.3);  | Proficient students identify coordinates when a sequence of rotations, reflections, translations, or dilations are performed in the coordinate plane (8.G.3); | Advanced students explain the sequence of rotations, reflections, translations, and dilations performed on the pre-image to determine the image (8.G.3);  |
|  | Basic students identify similarity from a sequence of transformations (8.G.4);  | Proficient students describe the properties of similarity between two figures when transformations are performed (8.G.4);                                     | Advanced students describe the property of similarity with triangles when identifying and establishing the Angle-Angle (AA) criterion for the triangles (8.G.5).  |
|  | Basic students determine the interior angle measure(s) of a triangle (8.G.5);   | Proficient students determine the interior and exterior angle measures of a triangle (8.G.5);   |   |
|  | Basic students identify the types of angles created when parallel lines are cut by a transversal (8.G.5).                   | Proficient students determine the measurement of angles or properties of angles that are created when parallel lines are cut by a transversal (8.G.5).        |   |
| <b>Range PLD: Cluster H -</b><br>Understand and apply the Pythagorean theorem.   | Basic students apply the Pythagorean Theorem in mathematical problems by setting up the equation $a^2 + b^2 = c^2$ (8.G.7). | Proficient students calculate the unknown side lengths in right triangles in real-world and mathematical problems (8.G.7);                                    | Advanced students explain and identify the proofs of the Pythagorean Theorem and the converse of the Pythagorean Theorem (8.G.6);   |
|  |   | Proficient students calculate the distance between two points on a grid by applying the Pythagorean Theorem (8.G.8).  | Advanced students calculate the distance between two points by applying the distance formula.   |
| <b>Range PLD: Cluster I -</b><br>Solve real-world and mathematical problems involving volume of cylinders, cones, and spheres.     | Basic students identify the formulas for the volumes of cones, cylinders, and spheres (8.G.9).                              | Proficient students calculate the volumes of a cone, cylinder, or sphere as a decimal value or in terms of pi (8.G.9).  | Advanced students solve for a component part (radius or height) given the volume of a cone, cylinder, or sphere and determine the volume of a composite figure containing two to more cones, cylinders, or spheres (8.G.9). |

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| <b>Domain</b>   | <b>Statistics and Probability</b>  |   |   |
| <b>Range PLD: Cluster J -</b><br>Investigate patterns of association in bivariate data. | Basic students identify the pattern of association in scatter plots as a positive association, negative association, or no association (8.SP.1); | Proficient students identify the pattern of association as a positive association, negative association, or no association given data in a table and describe characteristics of scatter plots such as clustering, outliers, and linear versus non-linear association (8.SP.1); | Advanced students identify the pattern of association given a verbal description as a positive association, negative association, or no association (8.SP.1); |
|   |  | Proficient students identify a line of best fit for scatter plots (8.SP.2);   | <b>Advanced students graph a curve of best fit for scatter plots;</b>   |
|   | Basic students use the equation of a linear model in the context of data to identify slope and intercepts (8.SP.3);                              | Proficient students use the equation of a linear model in the context of data to interpret the meaning of the slope and intercepts (8.SP.3);  | Advanced students use the data in a scatter plot to create an equation of a line of best fit (8.SP.3);  |
|   | Basic students identify values from a two-way table (8.SP.4).  | Proficient students interpret the data numerically in a two-way table (8.SP.4).   | Advanced students justify conclusions about the frequencies and relative frequencies of data in a two-way table (8.SP.4).                                     |